

# Observations of submesoscale eddies using high-frequency radar-derived kinematic and dynamic quantities

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(Kim, S. Y. 2010, *Cont. Shelf Res.* 30, 1639 -1655)

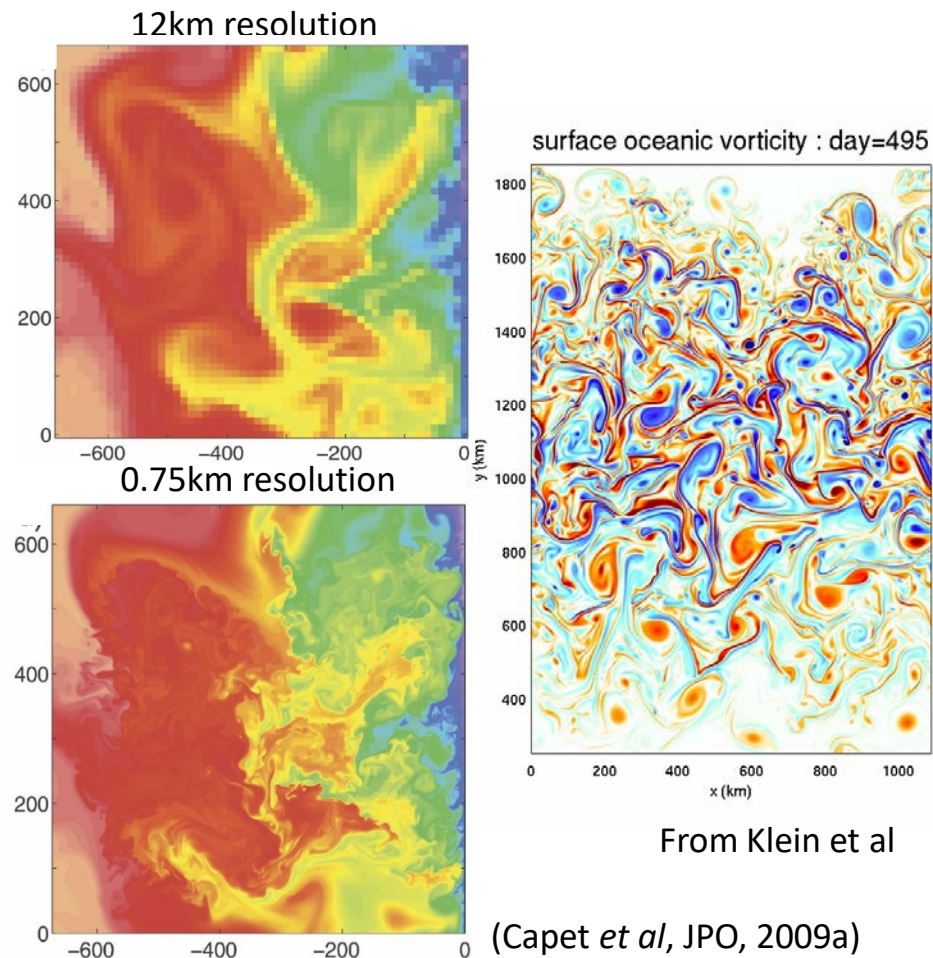
Acknowledgement: Eric Terrill and Bruce Cornuelle (SIO)



# Observations of **submesoscale eddies** using high-frequency radar-derived kinematic and dynamic quantities

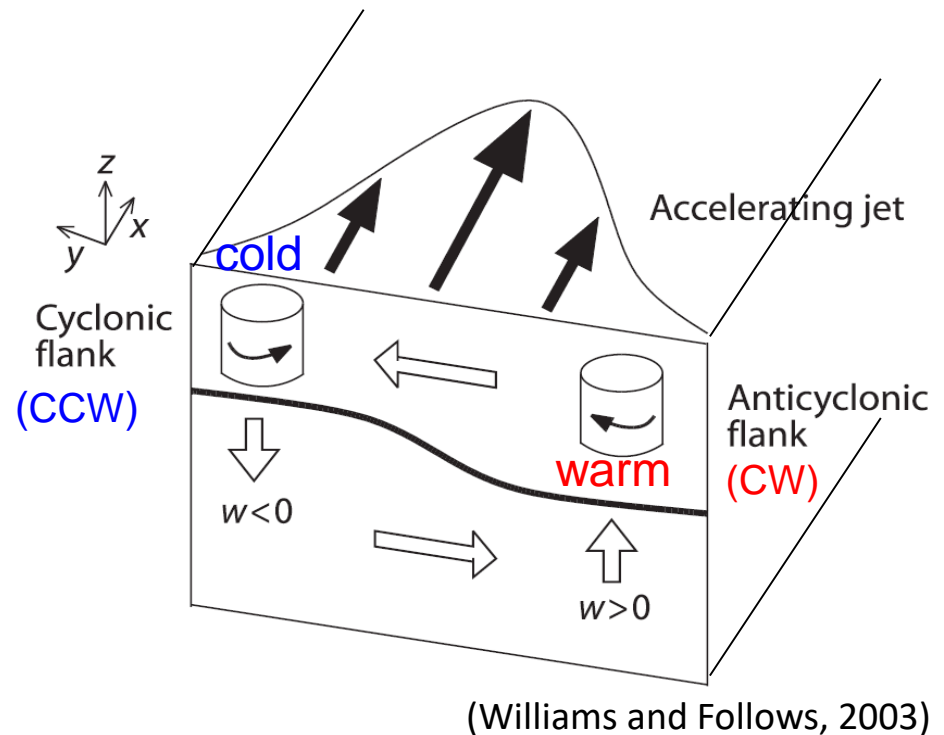
- Submesoscale processes
  - **O(1) Rossby number**  
[ $Ro = U/(fL) = \zeta/f$ ]
  - A horizontal scale smaller than the first baroclinic Rossby deformation radius; **O(1-10) km**
  - Frequently observed as fronts, **eddies**, and filaments

Simulations on mesoscale and submesoscale grids (SST)



# Observations of **submesoscale eddies** using high-frequency radar-derived kinematic and dynamic quantities

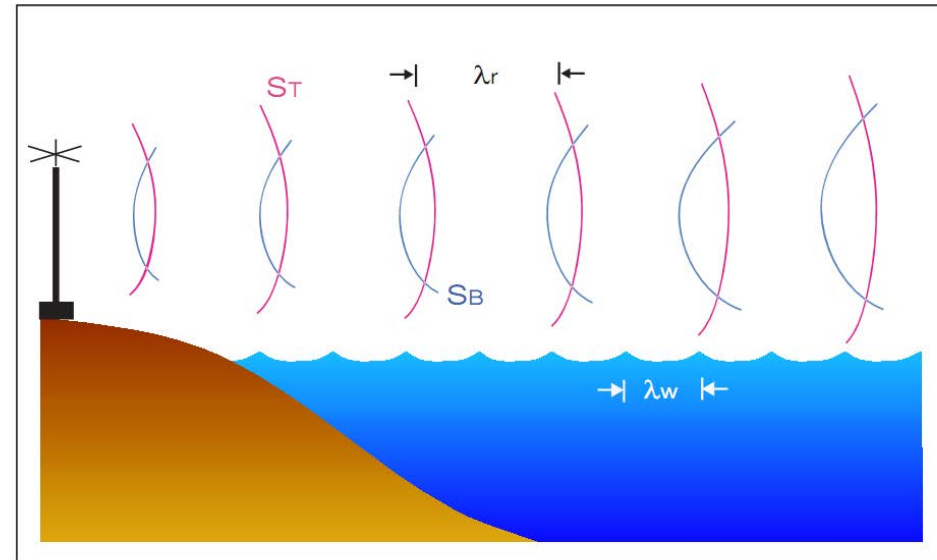
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  - $O(1)$  Rossby number  
[ $Ro = U/(fL) = \zeta/f$ ]
  - A horizontal scale smaller than the first baroclinic Rossby deformation radius;  $O(1-10)$  km
  - Frequently observed as fronts, eddies, and filaments
  - Contribute to the **vertical transport** of oceanic tracers, mass, and buoyancy and **rectify the mixed-layer structure and upper-ocean stratification**



e.g., vertical frontal scale secondary circulation

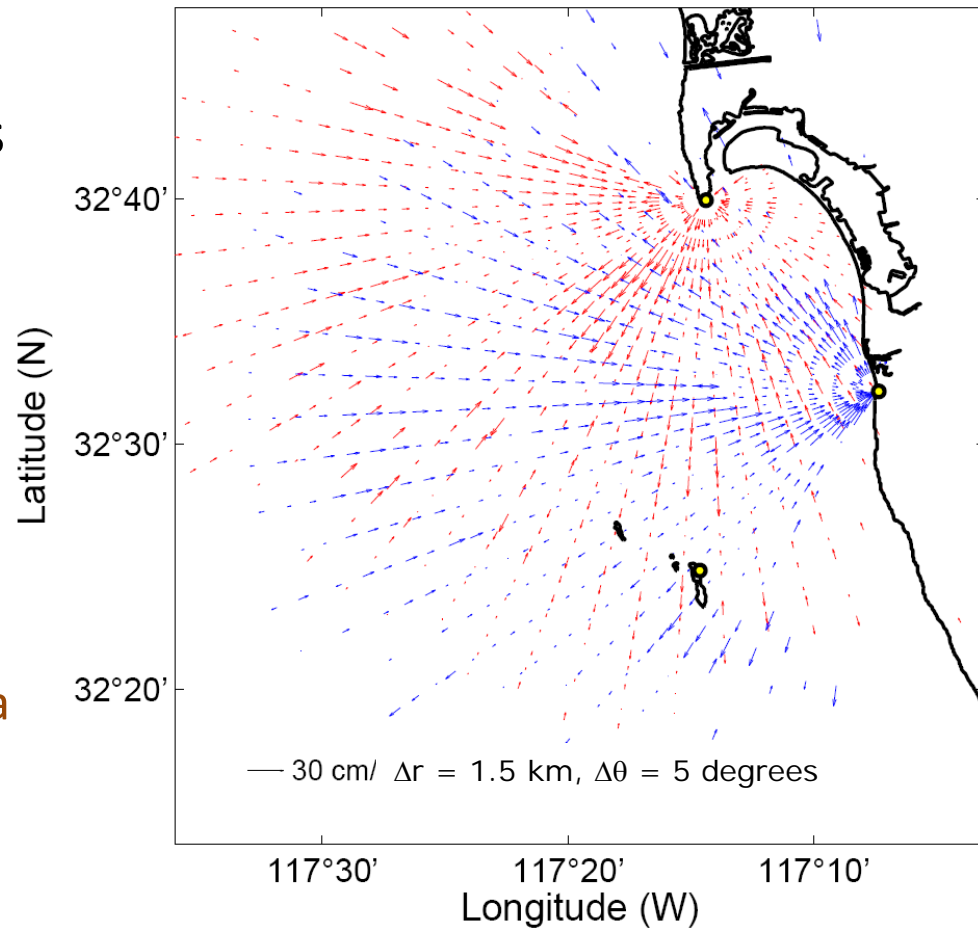
# Observations of submesoscale eddies using high-frequency radar-derived kinematic and dynamic quantities

- An observational sensor using electromagnetic waves
  - 3-30 MHz frequency (HFR)
  - Using Doppler shift of backscattered signals of surface gravity waves to estimate the background currents
  - Upper 1 m depth-averaged currents



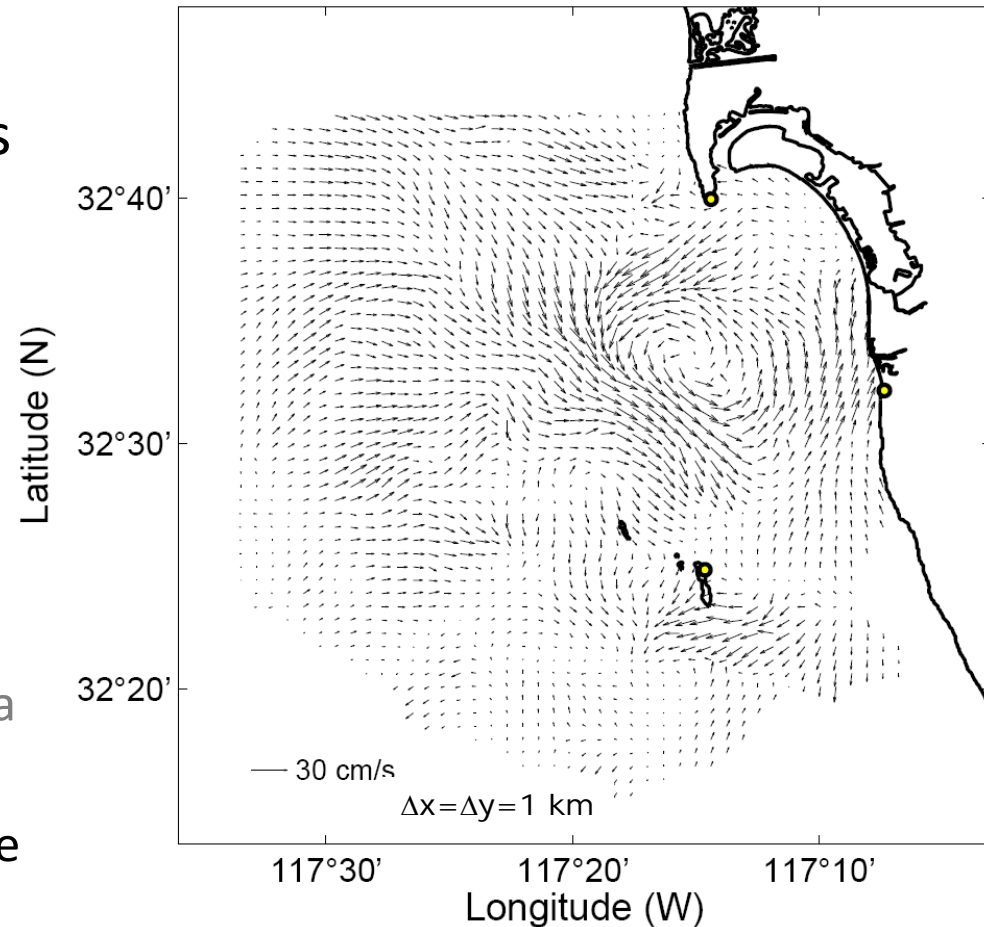
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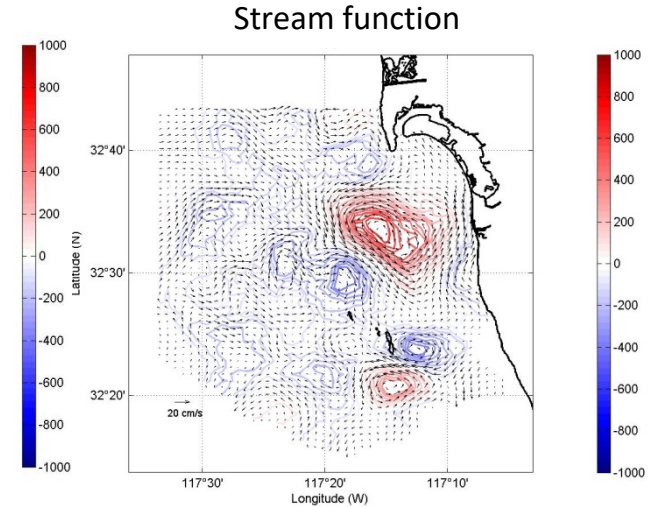
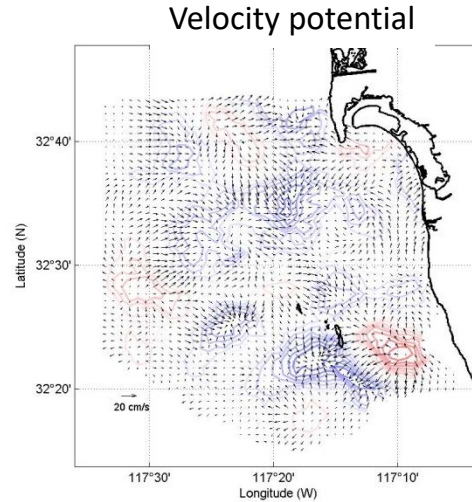
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  - Hourly and O(1) km scale surface current maps



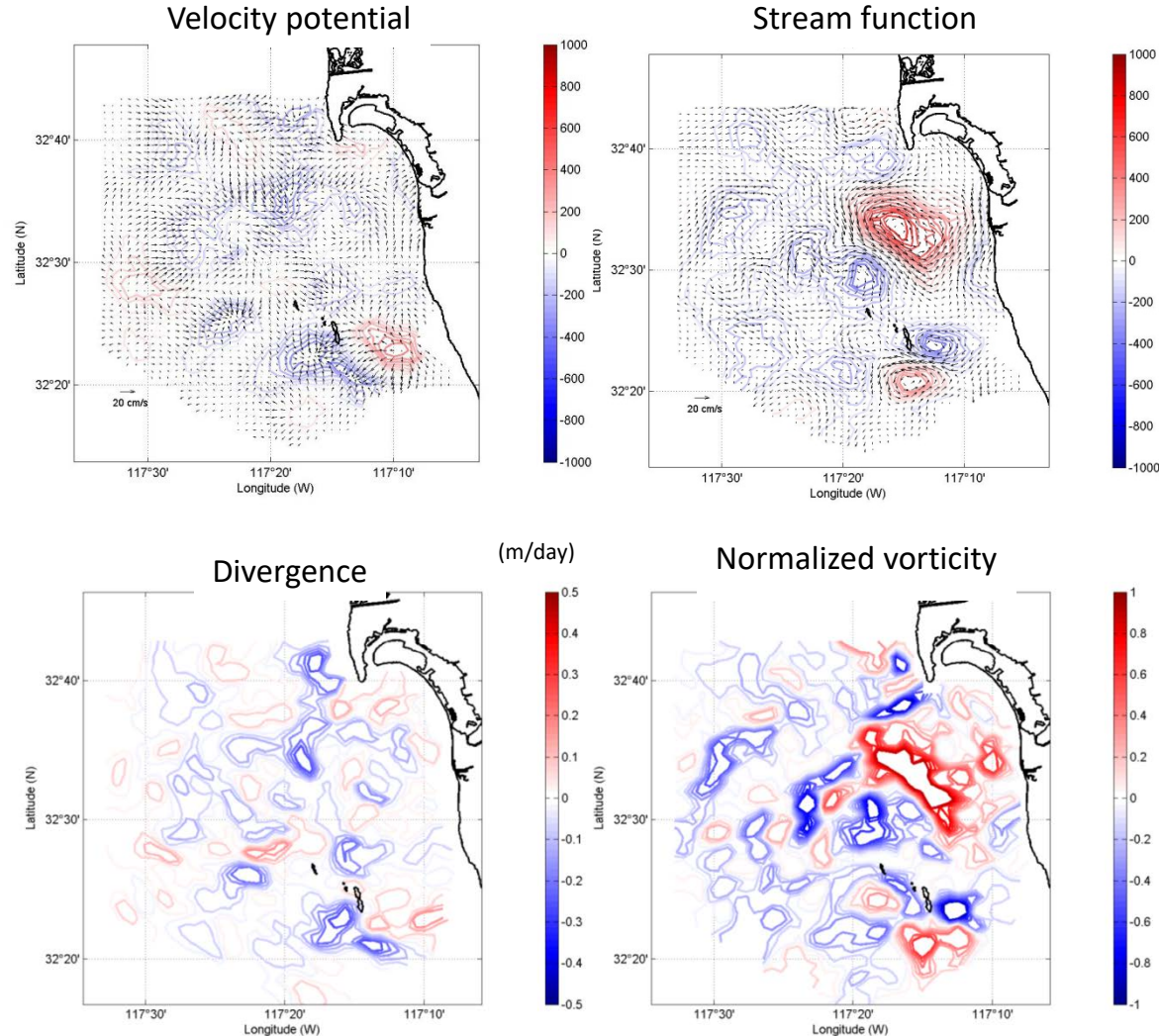
# Observations of submesoscale eddies using high-frequency radar-derived kinematic and dynamic quantities

- Velocity potential  
and stream function



# Observations of submesoscale eddies using high-frequency radar-derived kinematic and dynamic quantities

- Velocity potential and stream function
- Divergence and normalized vorticity





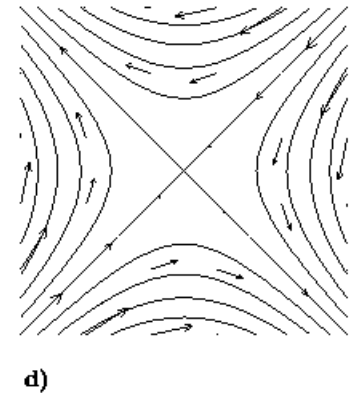
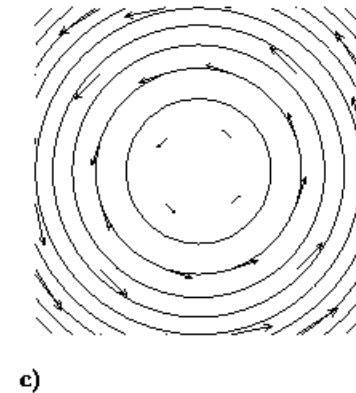
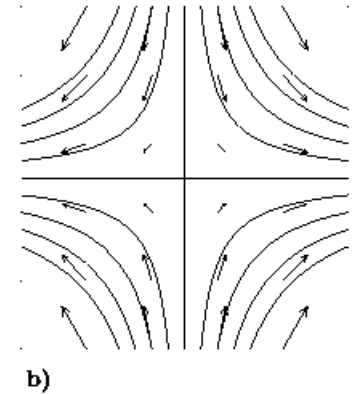
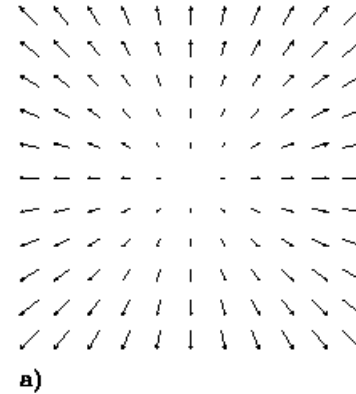
# Observations of submesoscale eddies using high-frequency radar-derived kinematic and dynamic quantities

- Velocity potential and stream function
- Divergence and normalized vorticity
- Stretching and shearing deformation rates, and strain rate

$$Q = \frac{\partial v}{\partial x} + \frac{\partial u}{\partial y},$$

$$\zeta = \frac{\partial u}{\partial x} - \frac{\partial v}{\partial y},$$

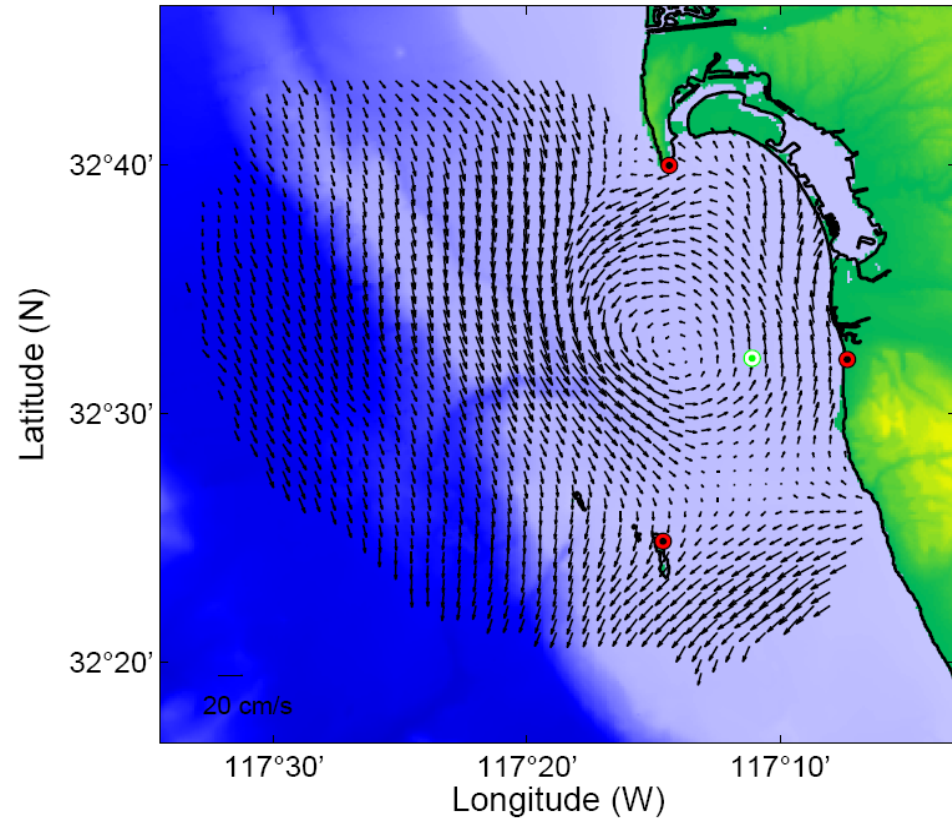
$$\kappa = \sqrt{Q^2 + \zeta^2}.$$



(a) divergence; (b) stretching deformation;  
(c) vorticity; (d) shearing deformation.

# Observations of submesoscale eddies using high-frequency radar-derived kinematic and dynamic quantities

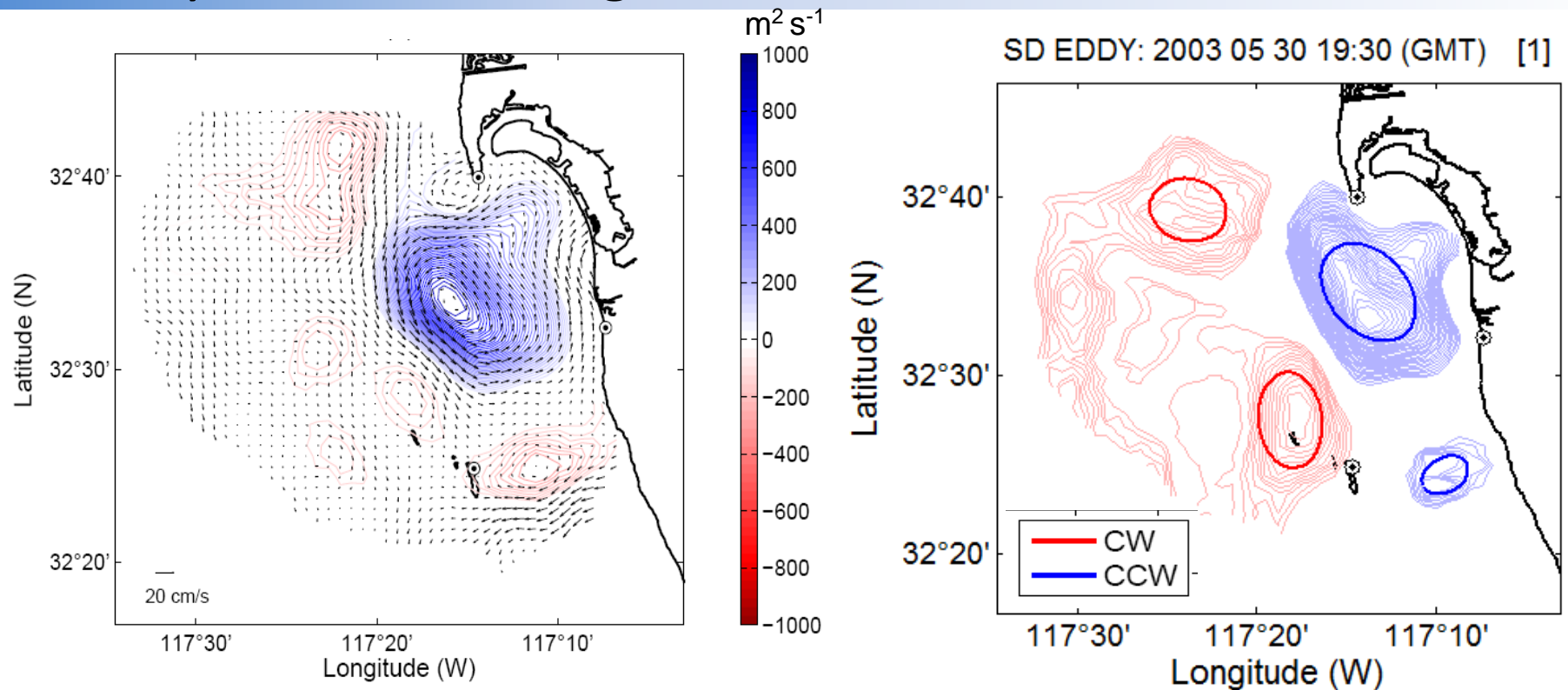
- Surface
  - Hourly and O(1) km resolution surface current maps
  - Their kinematic and dynamic quantities
- Subsurface
  - ADCP – current profiles
  - Temperature profiles – vertical movement of thermoclines



## Outline for rest of the talk...

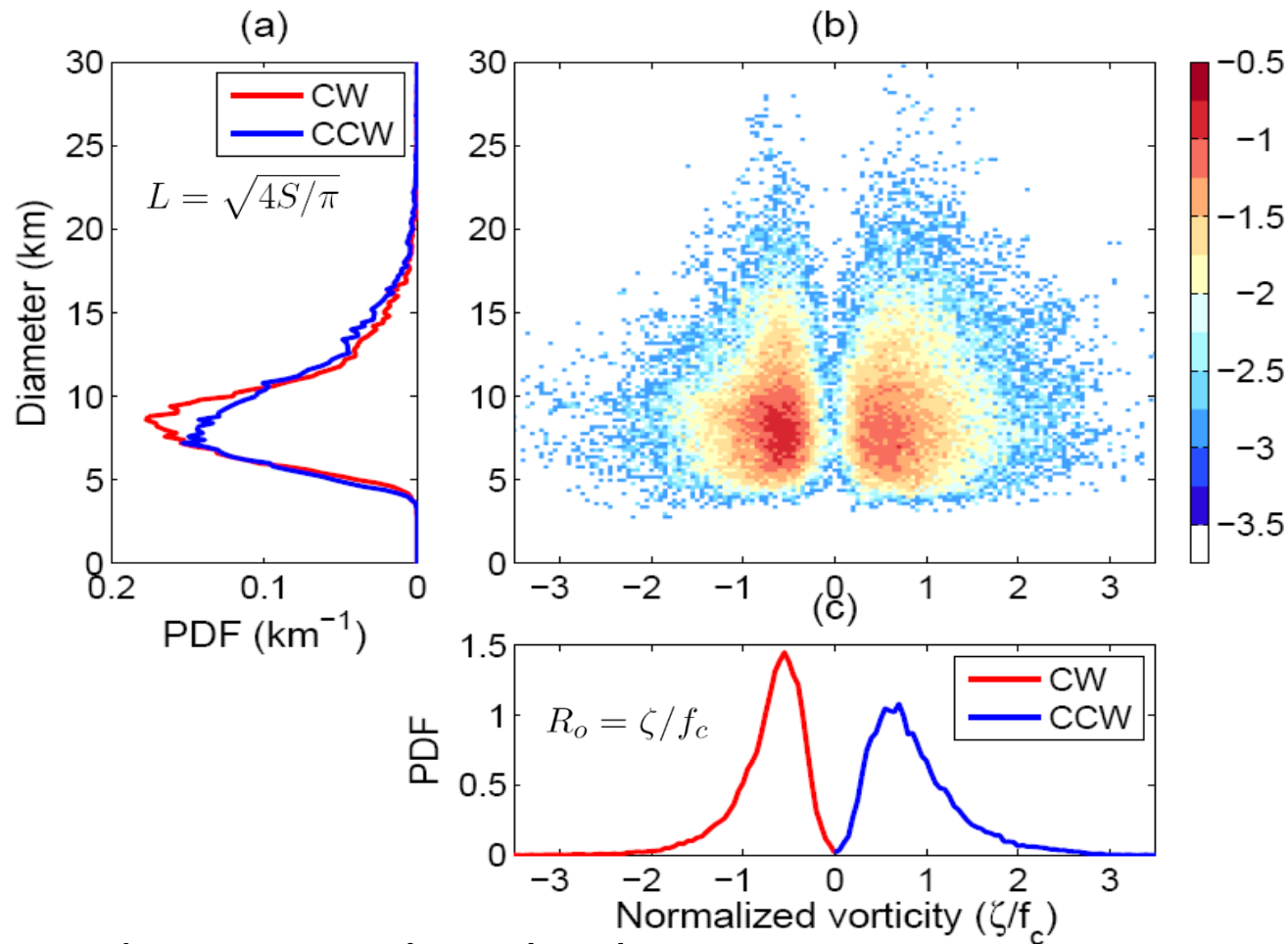
- Eddy detection using surface current maps
  - Geometry-based technique
- Interpretation of submesoscale eddies
  - Statistics of diameters and Rossby numbers
  - Verification with circulation
  - Horizontal structure of identified eddies
  - Secondary circulation due to drifting submesoscale eddies
- Summary

# Eddy detection using HFR surface currents



- Streamlines (nearly closed polygons) are identified with winding angle method.
- Co-centered streamlines are fitted into an ellipse.
- If the centers of ellipses in consecutive time steps are within a drifting range (e.g., 1.5 km) with the same rotation, ellipses are considered as a part of an eddy time series. The length of time series is called as persistency.

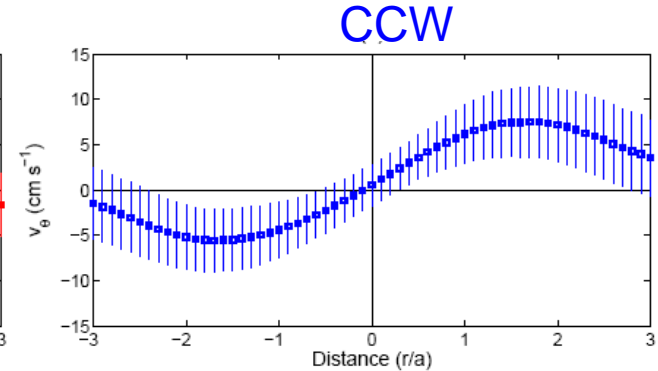
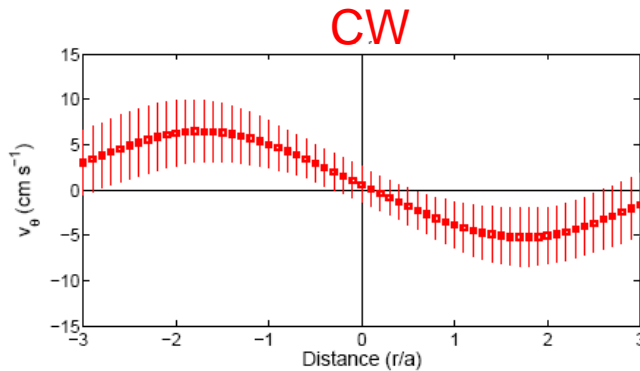
# Rossby number and size



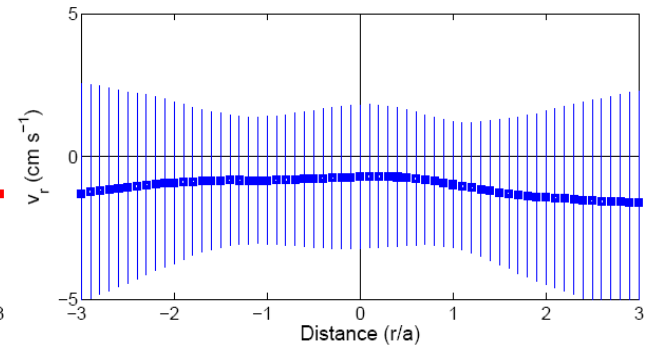
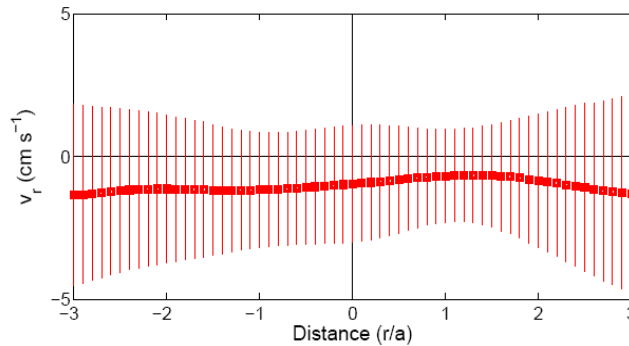
- Based on 2-year hourly observations.
- About 700 eddies are identified for each rotation
- $O(0.5-1)$  Rossby number at the center of eddies
- 5 – 20 km size diameter ( $L$ ) eddies

# Horizontal structure

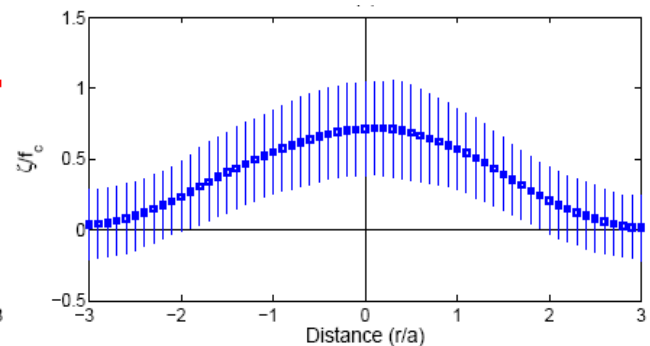
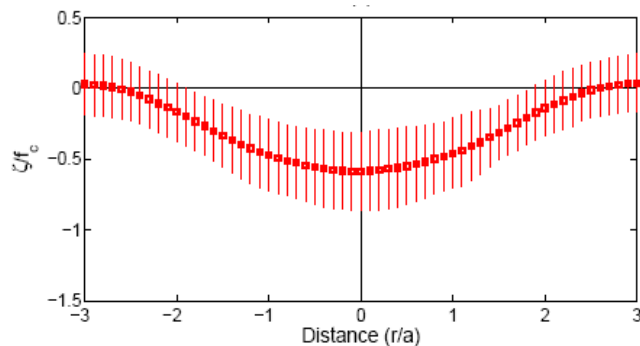
$V_{\Theta}$   
Tangential  
velocity



$V_r$   
Radial  
velocity



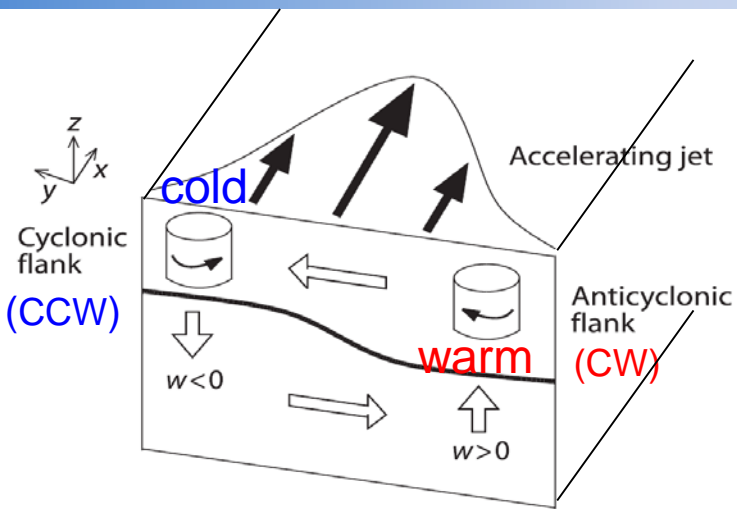
$\zeta/f_c$   
Rossby  
number



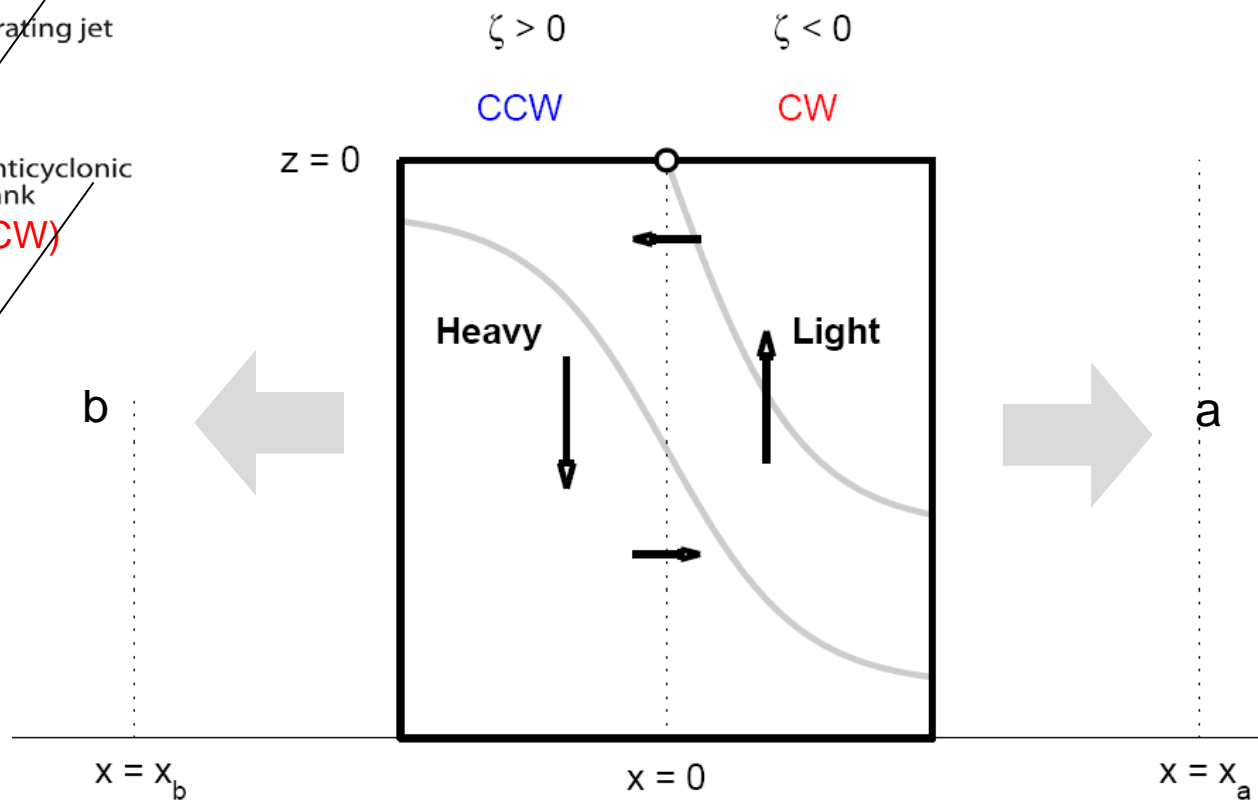
$r/a$ : Relative distance on the major axis

- $V_{\Theta}$  and  $\zeta/f_c$  have similar shapes to the Taylor eddy.

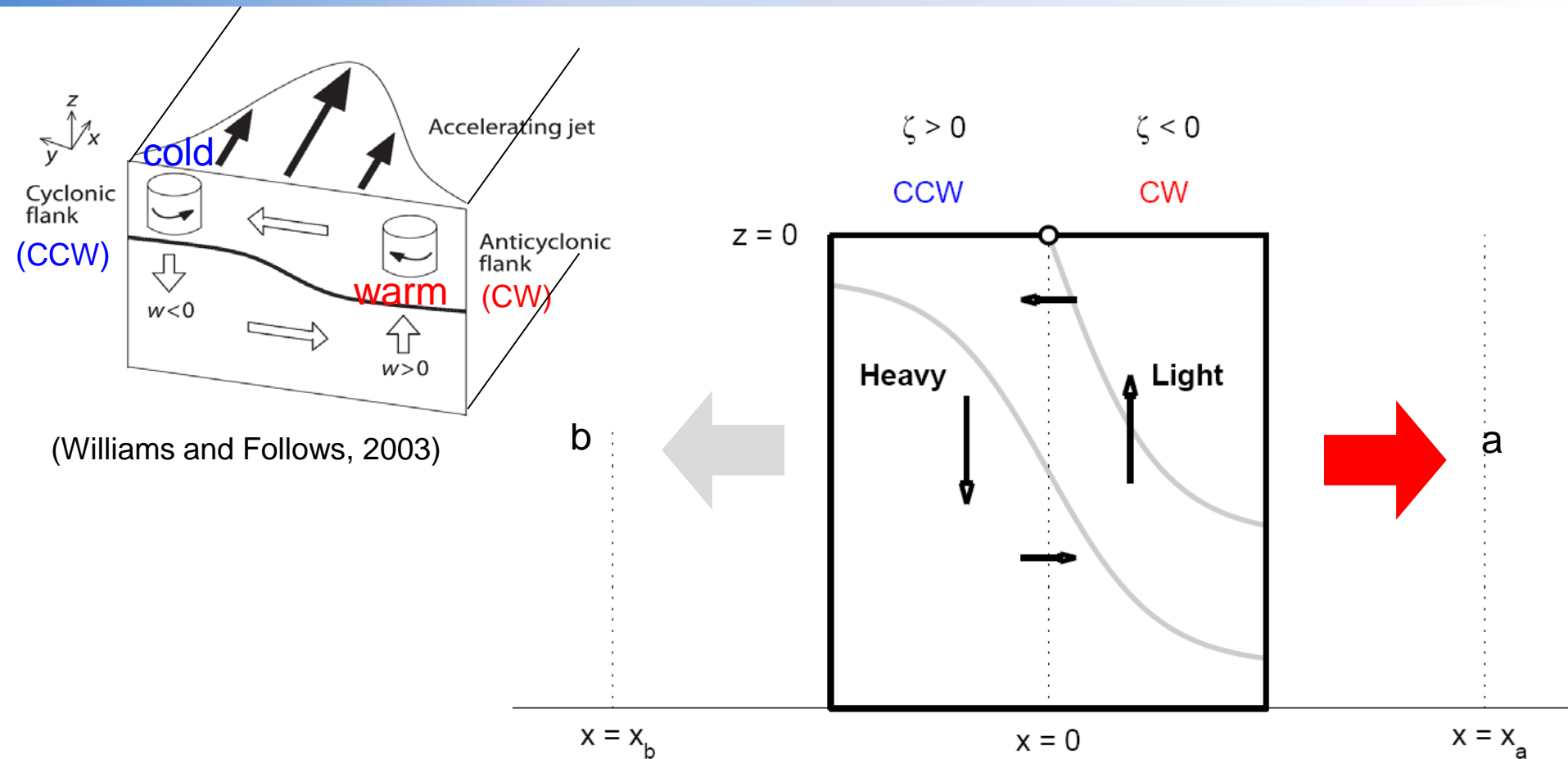
# Frontal-scale secondary circulation: Expectation



(Williams and Follows, 2003)



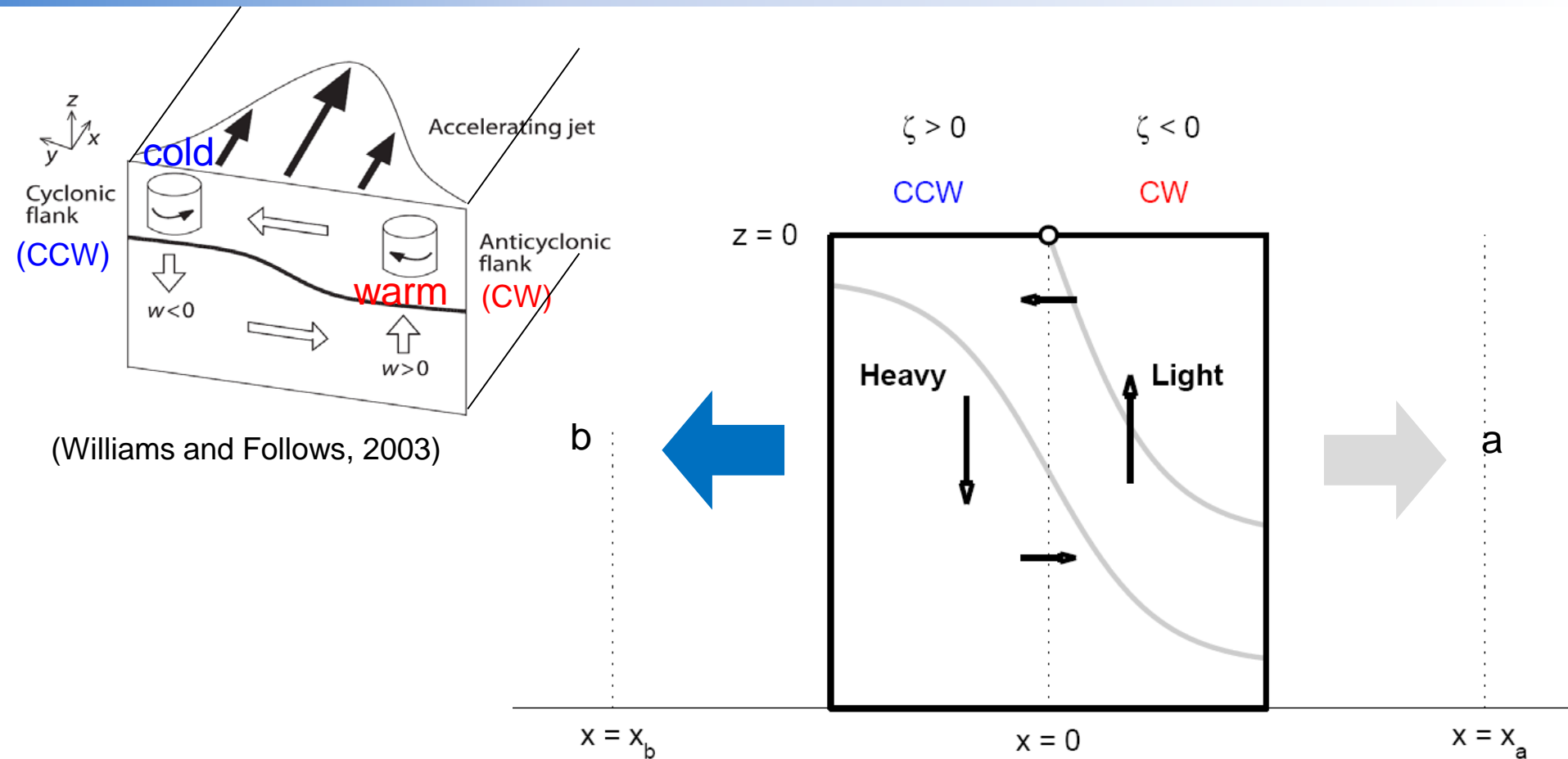
# Frontal-scale secondary circulation: Expectation



- Paired eddies (a front) move to 'a', thermoclines fluctuate up- and down-ward.



# Frontal-scale secondary circulation: Expectation



- Paired eddies (a front) move to 'a', thermoclines fluctuate up- and down-ward.
- On the other hand, due to moving paired eddies (front) to 'b', the thermoclines fluctuate down- and up-ward.

# Frontal-scale secondary circulation: Data-derived indicator

## • Surface

- Stream function, velocity potential
- Divergence and vorticity,
- Shearing and stretching deformation rates, and strain rate

$$\delta = \nabla_H \cdot \mathbf{u} = \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y},$$

$$\zeta = \nabla_H \times \mathbf{u} = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y},$$

$$\varrho = \frac{\partial v}{\partial x} + \frac{\partial u}{\partial y},$$

$$\varsigma = \frac{\partial u}{\partial x} - \frac{\partial v}{\partial y},$$

$$\kappa = \sqrt{\varrho^2 + \varsigma^2}.$$

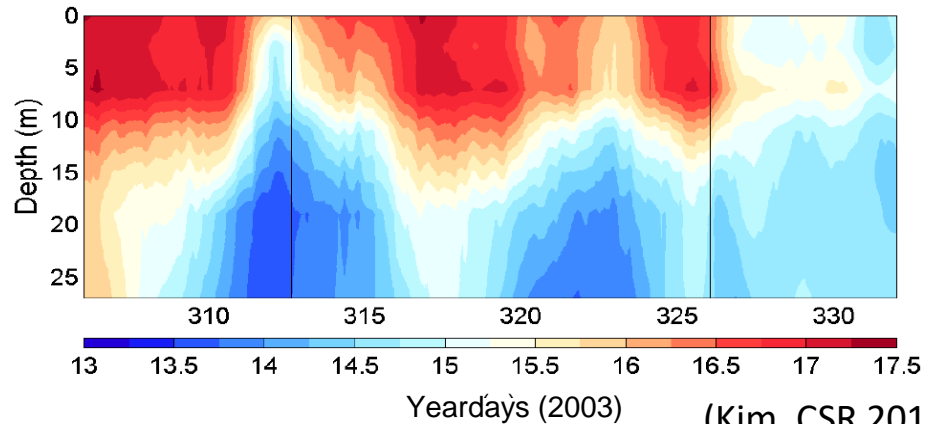
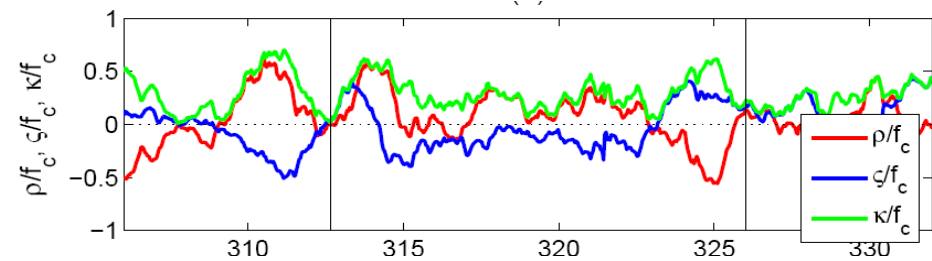
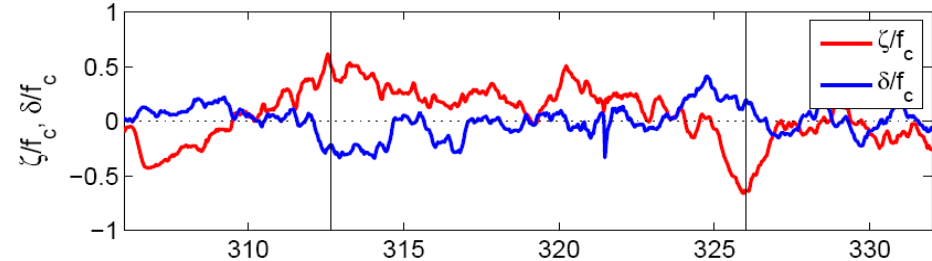
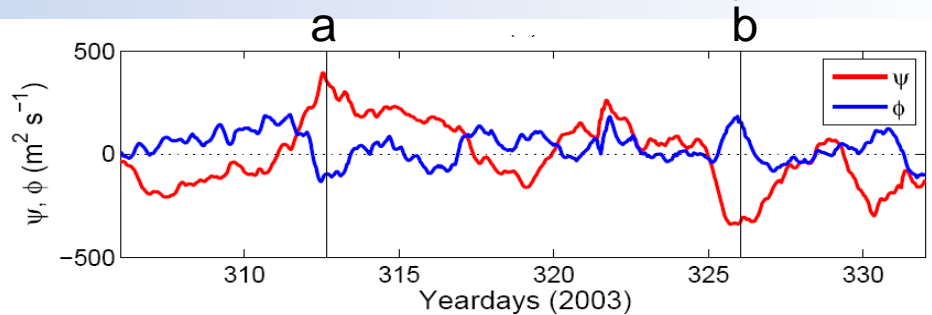
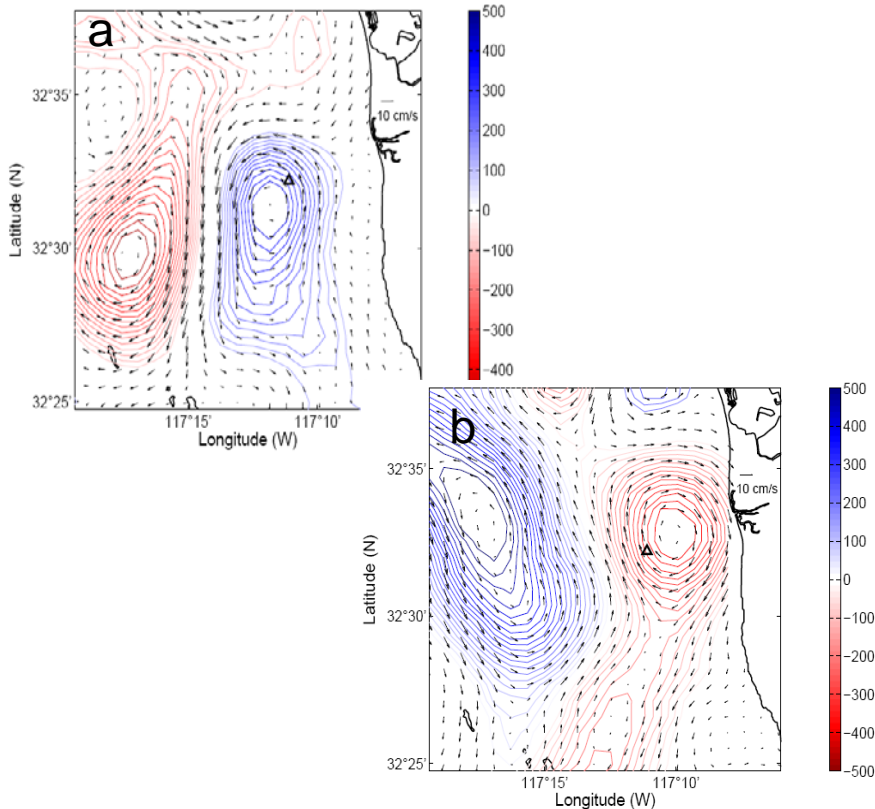
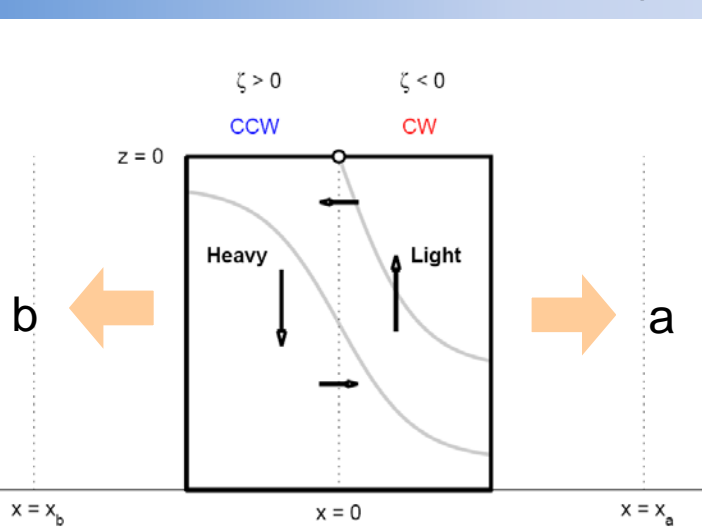
## • Subsurface

- ADCP Current profiles [ $\mathbf{u} = \mathbf{u}(z, t)$ ]
- Rotational tendency of the whole water column: Vertical rotary coefficients

$$\alpha(t) = \frac{-\sum_{m < 0} S(m,t) + \sum_{m > 0} S(m,t)}{\sum_{m < 0} S(m,t) + \sum_{m > 0} S(m,t)},$$

- Vertical movements of thermoclines [T-string data]

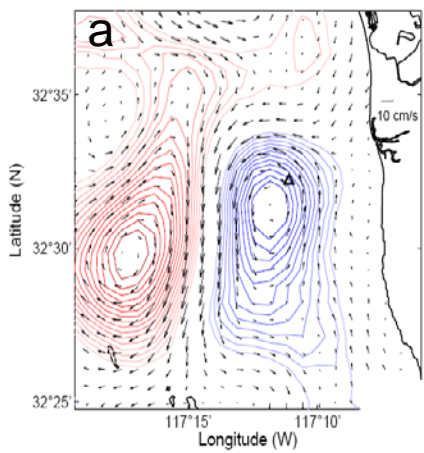
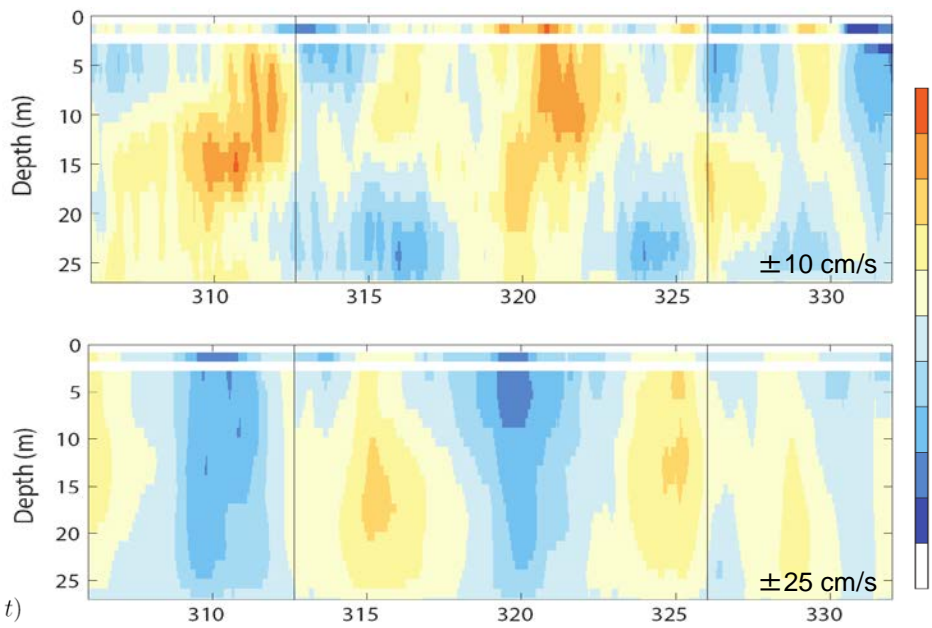
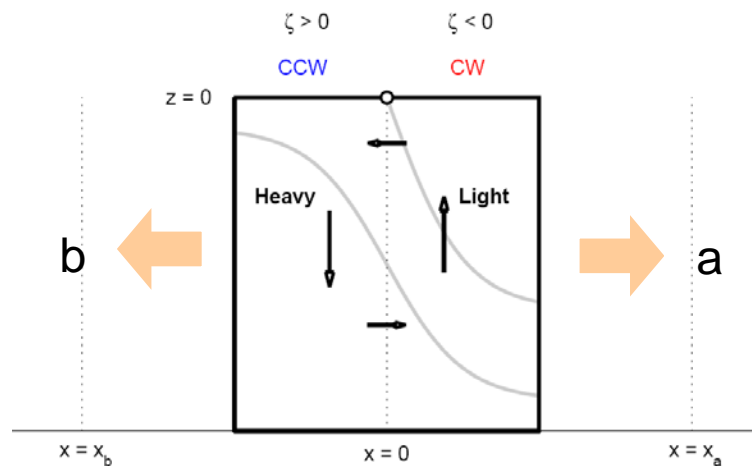
# Frontal-scale secondary circulation: Surface & Temp.



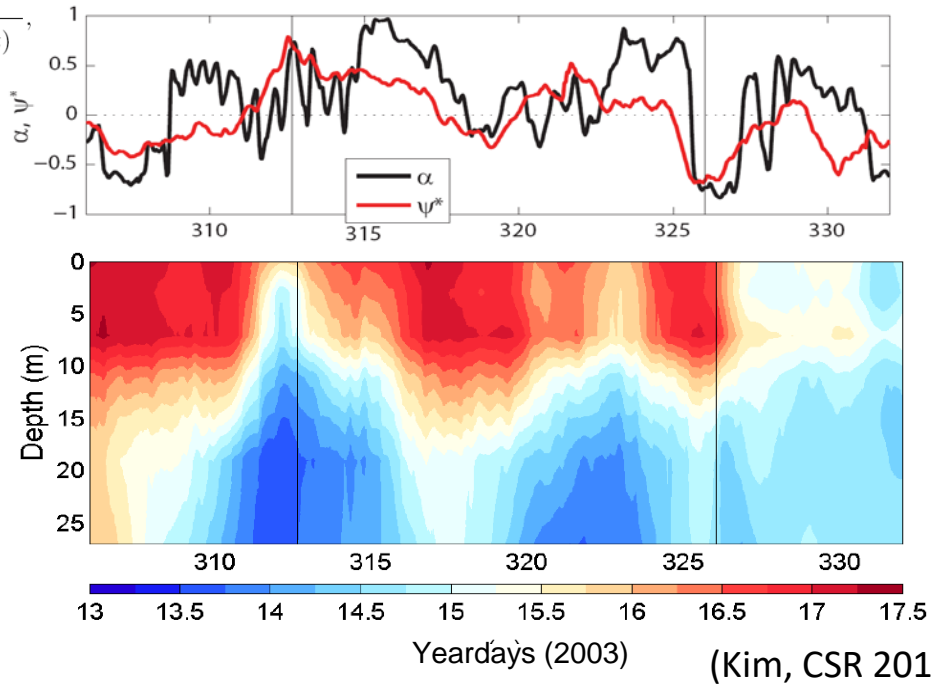
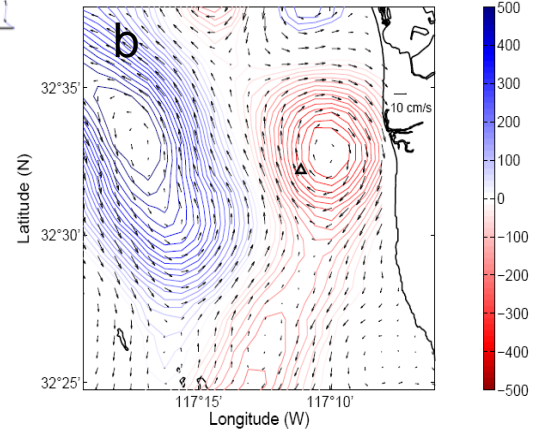
# Frontal-scale secondary circulation: Subsurface & Temp

a

b



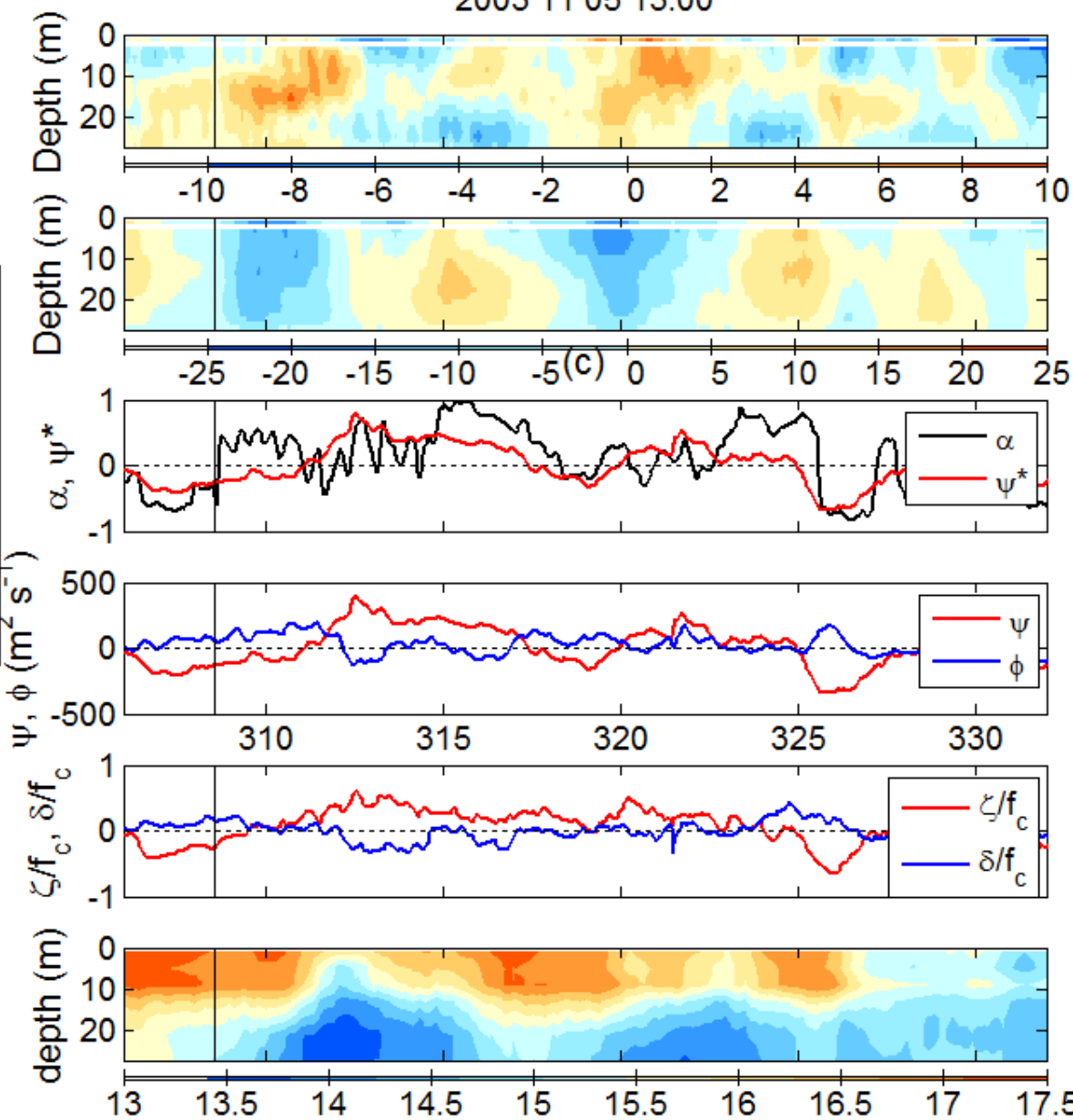
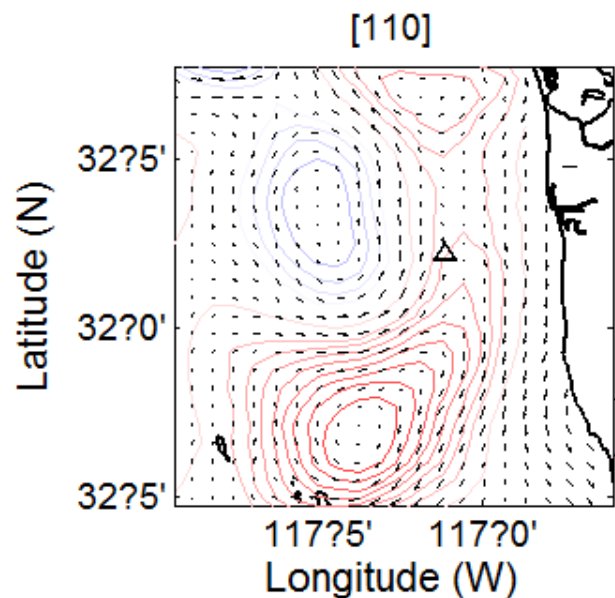
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(Kim, CSR 2010)

# Two events of submesoscale eddies approaching ADCP/T-string

2003 11 05 13:00



# Summary

- **Submesoscale eddies** off southern San Diego detected from direct estimate of kinematic and dynamic quantities of HFR observations and ADCP: **Rossby number of  $O(0.5-1)$  and 5-25 km diameter**
- **Frontal-scale vertical circulation due to drifting eddies undulates thermoclines.**
- Available submesoscale observational resources are very sparse and few, but they may enhance our understanding on the submesoscale process studies including biological interactions.