



Several approaches to conduct quality assurance and quality control on the HFR radial velocity maps

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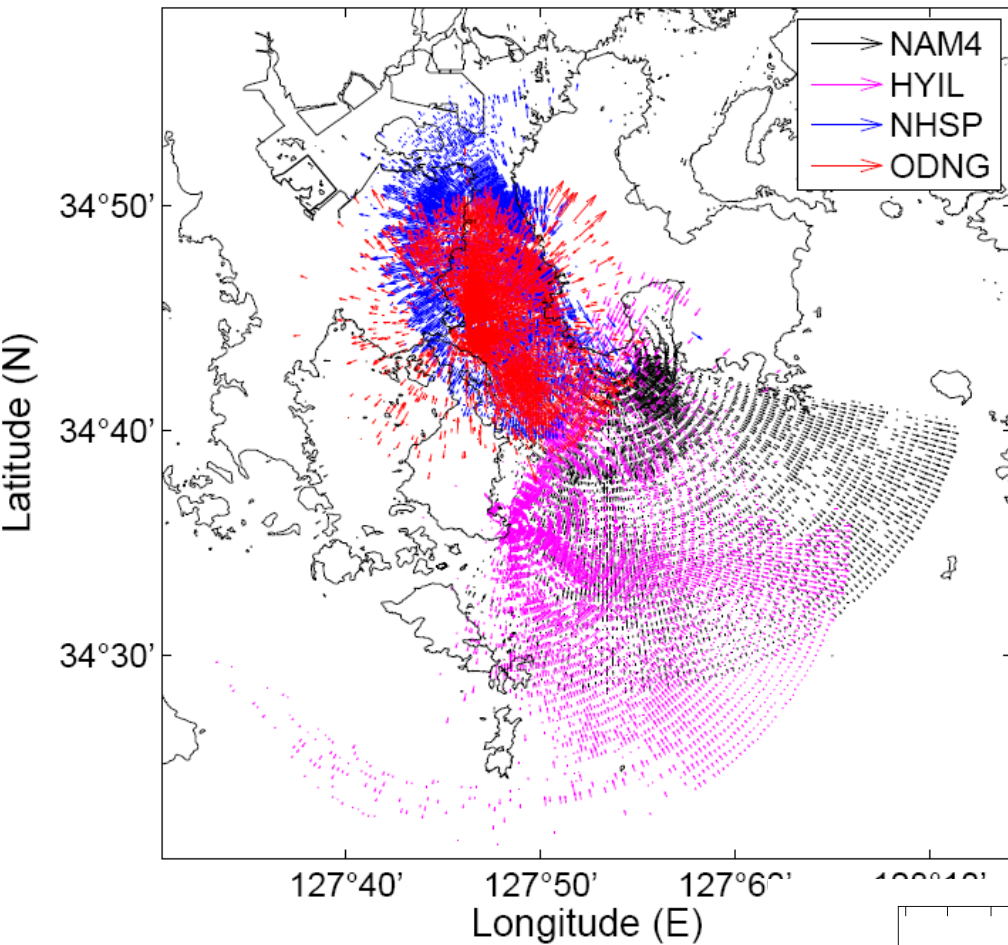
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Collaborators: S. H. Lee (Kunsan Nat'l Univ., Korea), KHOA, E. Terrill (SIO).

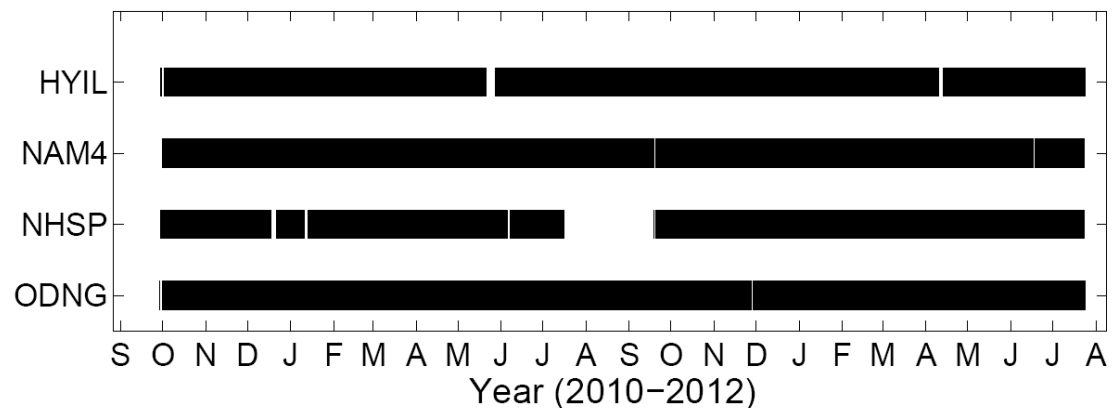
Outline

- QAQC of HF radar radial velocity maps (hindcast mode)
 - Spatial coverage of long term data
 - Correlation/covariance of pairs of radial velocities (RMS estimates)
 - 1 degree- vs 5 degree-azimuthal resolution?
 - RMS of difference of radial velocities (ideal vs. measured; CODAR only)
 $\|r_{\text{ideal}} - r_{\text{measured}}\|$
 - Geophysical signals
 - Energy spectra – tides, wind, inertial, and low-frequency forcing
 - Comparison with independent observations
 - Spatial coherence (correlation in a specific frequency band)
- Summary

Radial velocity maps (Yeosu, Korea)

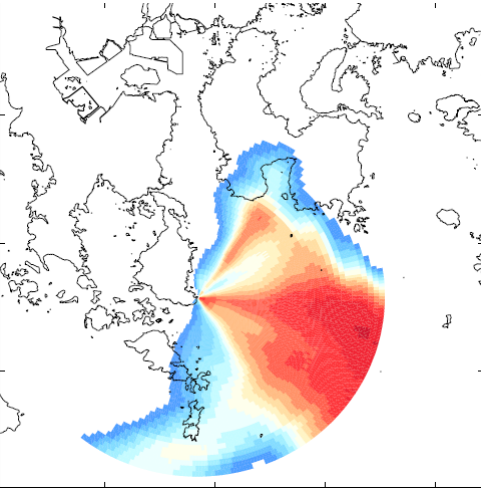


- 25MHz x 2;
42MHz x 2 (Yeosu, Korea)
- About two years hourly data

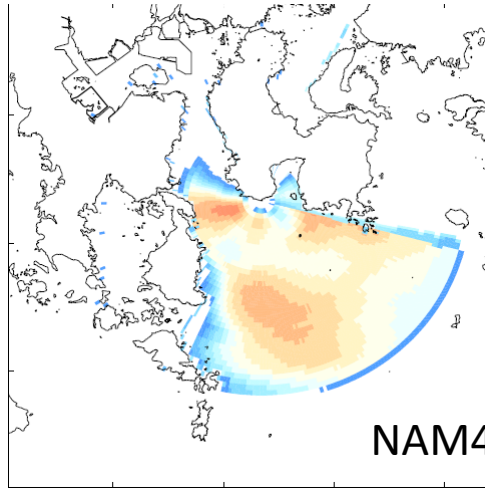


Spatial coverage of radial velocity maps (Yeosu, Korea)

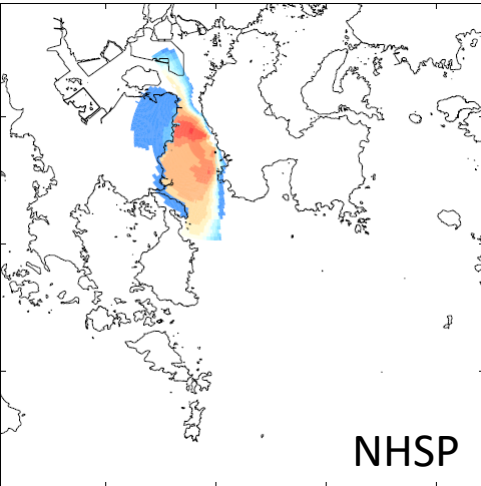
HYIL



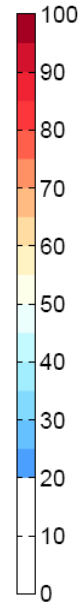
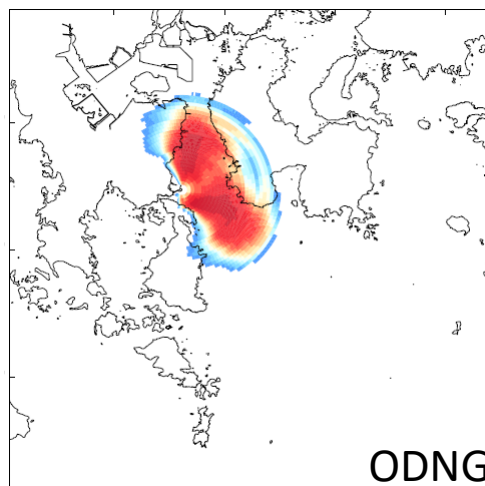
NAM4



NHSP



ODNG



- Long-term data coverage can provide the spatial consistency and influence/interference of coastline.

Correlation coefficients of pairs of radial velocities

$$r_1(t) = \mathbf{g}_1^T \mathbf{u}_1(t) + \epsilon_1(t) = u_1(t) \cos \theta_1 + v_1(t) \sin \theta_1 + \epsilon_1(t),$$

$$r_2(t) = \mathbf{g}_2^T \mathbf{u}_2(t) + \epsilon_2(t) = u_2(t) \cos \theta_2 + v_2(t) \sin \theta_2 + \epsilon_2(t),$$

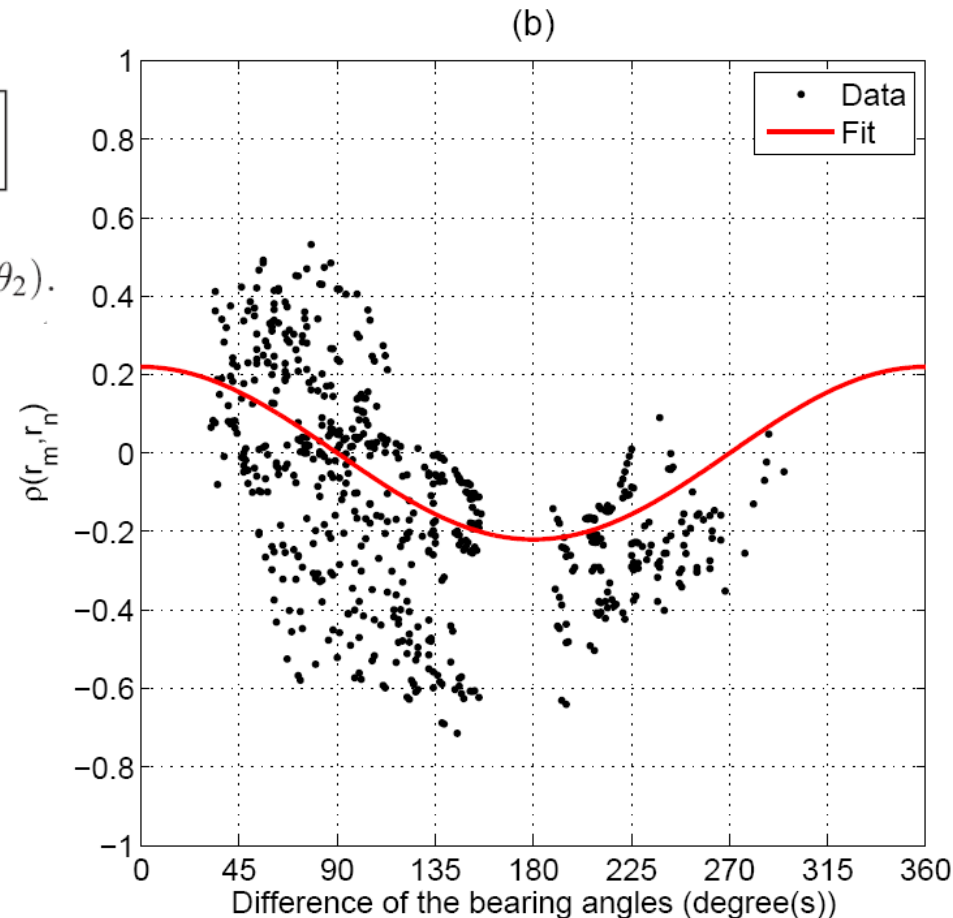
$$\langle r_1 r_2^T \rangle = \mathbf{g}_1^T \langle \mathbf{u}_1 \mathbf{u}_2^T \rangle \mathbf{g}_2 = [\cos \theta_1 \quad \sin \theta_1] \langle \mathbf{u}_1 \mathbf{u}_2^T \rangle \begin{bmatrix} \cos \theta_2 \\ \sin \theta_2 \end{bmatrix}$$

$$\langle r_1 r_2^T \rangle = \sigma^2 (\cos \theta_1 \cos \theta_2 + \sin \theta_1 \sin \theta_2) = \sigma^2 \cos(\theta_1 - \theta_2).$$

$$\rho(r_1, r_2) = \frac{\langle r_1 r_2^T \rangle}{\sqrt{\langle r_1^2 \rangle} \sqrt{\langle r_2^2 \rangle}} = \frac{\sigma^2}{\sigma^2 + \gamma^2} \cos(\theta_1 - \theta_2),$$

$$\text{where } \langle r_1^2 \rangle = \langle r_2^2 \rangle = \sigma^2 + \gamma^2 \text{ and } \langle \epsilon_1^2 \rangle = \langle \epsilon_2^2 \rangle = \gamma^2.$$

(Kim *et al*, JGR-C; 2010)

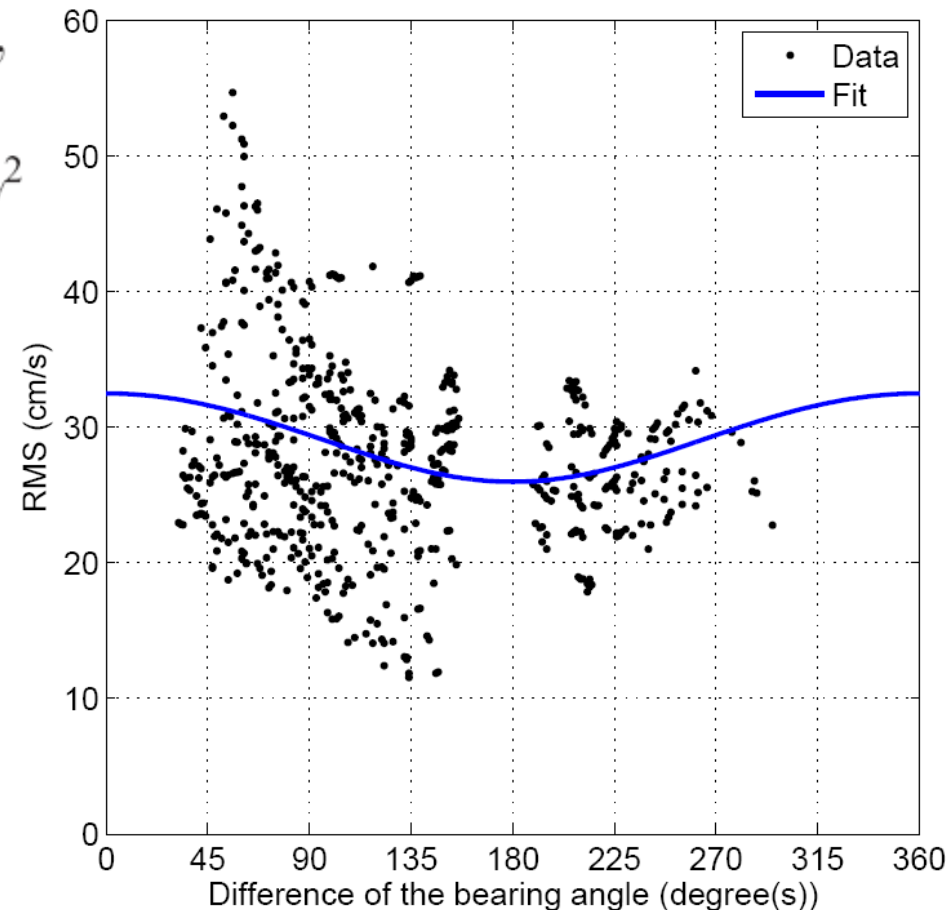


Covariance of pairs of radial velocities

$$\begin{aligned} \langle (r_1 + r_2)^2 \rangle \\ = \langle u^2 \rangle (\cos \theta_1 + \cos \theta_2)^2 + \langle v^2 \rangle (\sin \theta_1 + \sin \theta_2)^2 + \langle \epsilon_1^2 \rangle + \langle \epsilon_2^2 \rangle. \end{aligned}$$

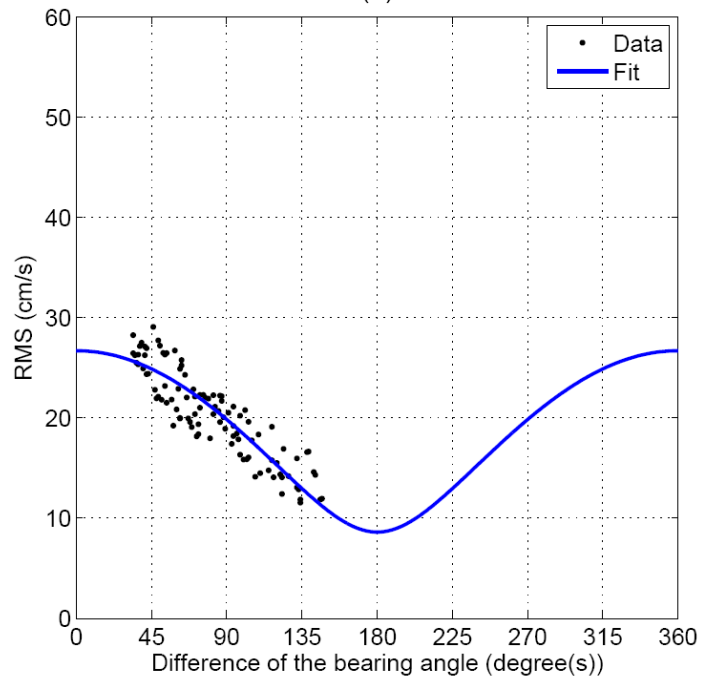
$$\langle u^2 \rangle = \langle v^2 \rangle = \sigma^2 \text{ and } \langle \epsilon_1^2 \rangle = \langle \epsilon_2^2 \rangle = \gamma^2,$$

$$\langle (r_1 + r_2)^2 \rangle = 4 \sigma^2 \cos^2 \left(\frac{\theta_1 - \theta_2}{2} \right) + 2 \gamma^2$$

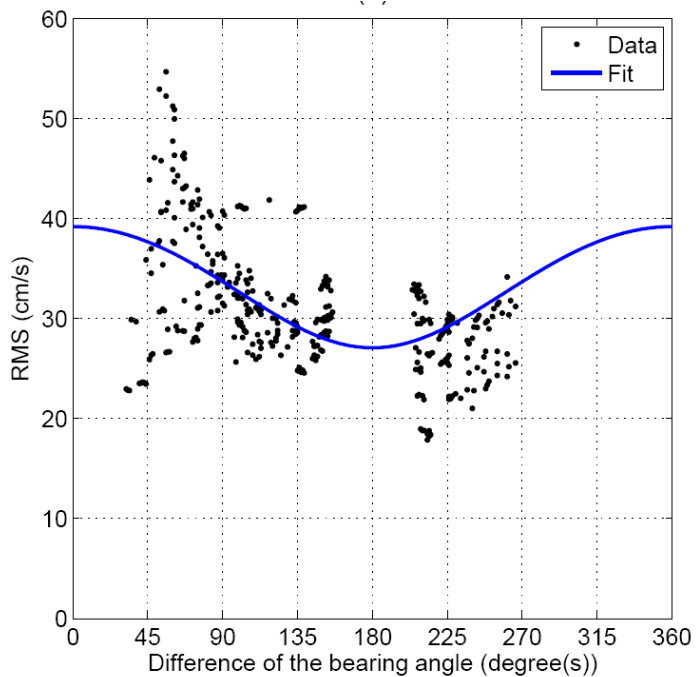
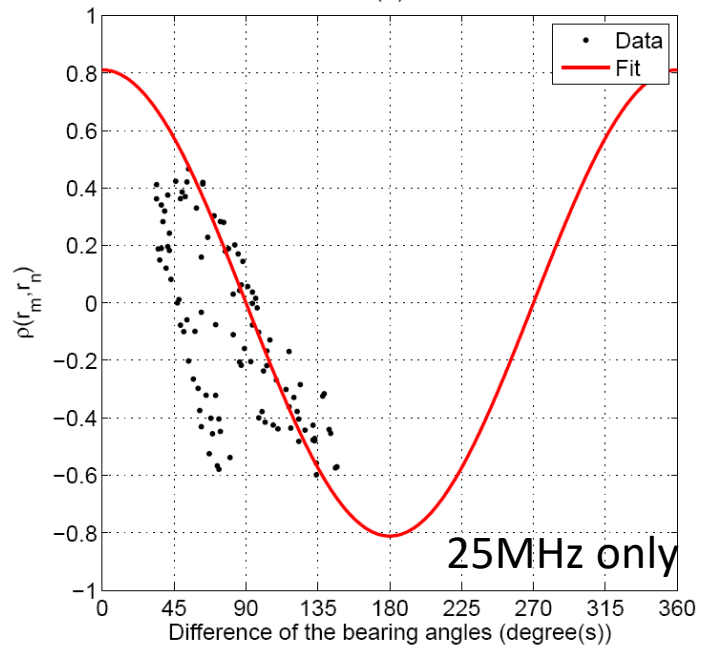


(Kim *et al*, JGR-C; 2010)

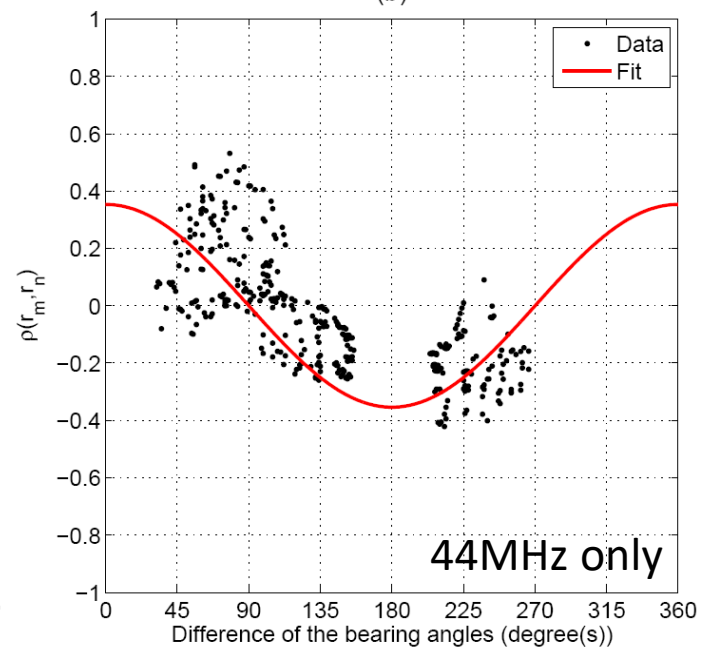
(a)



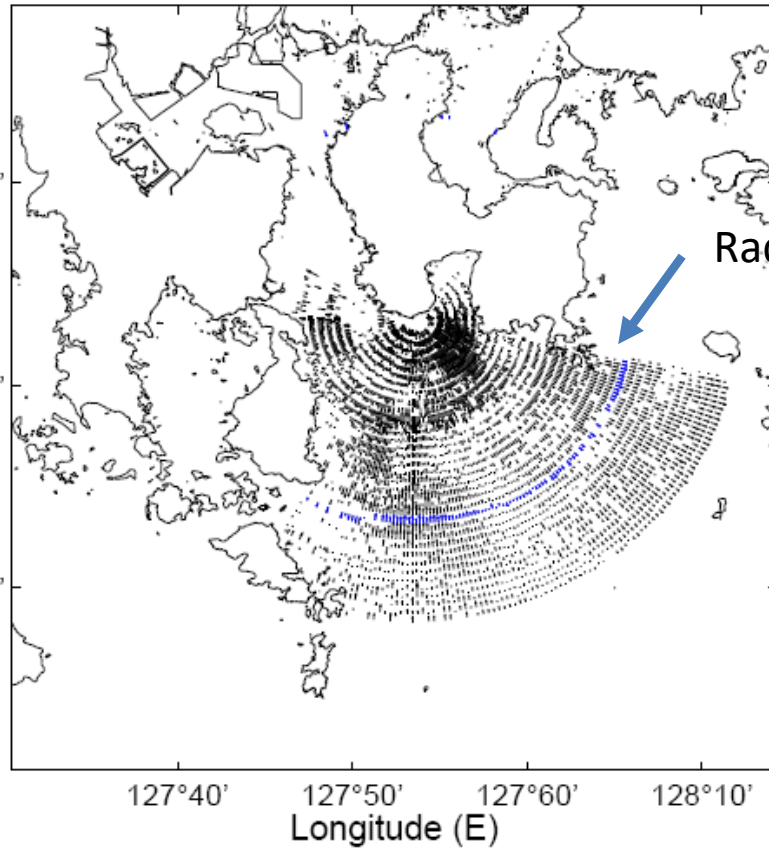
(b)



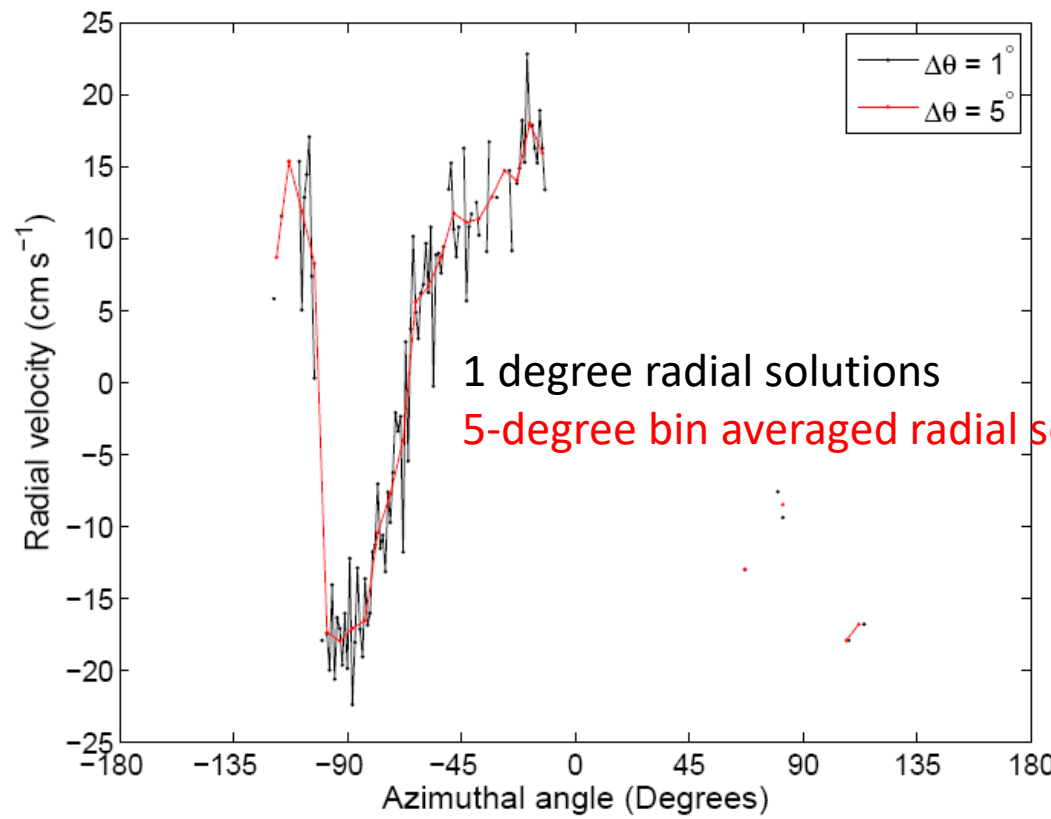
(b)



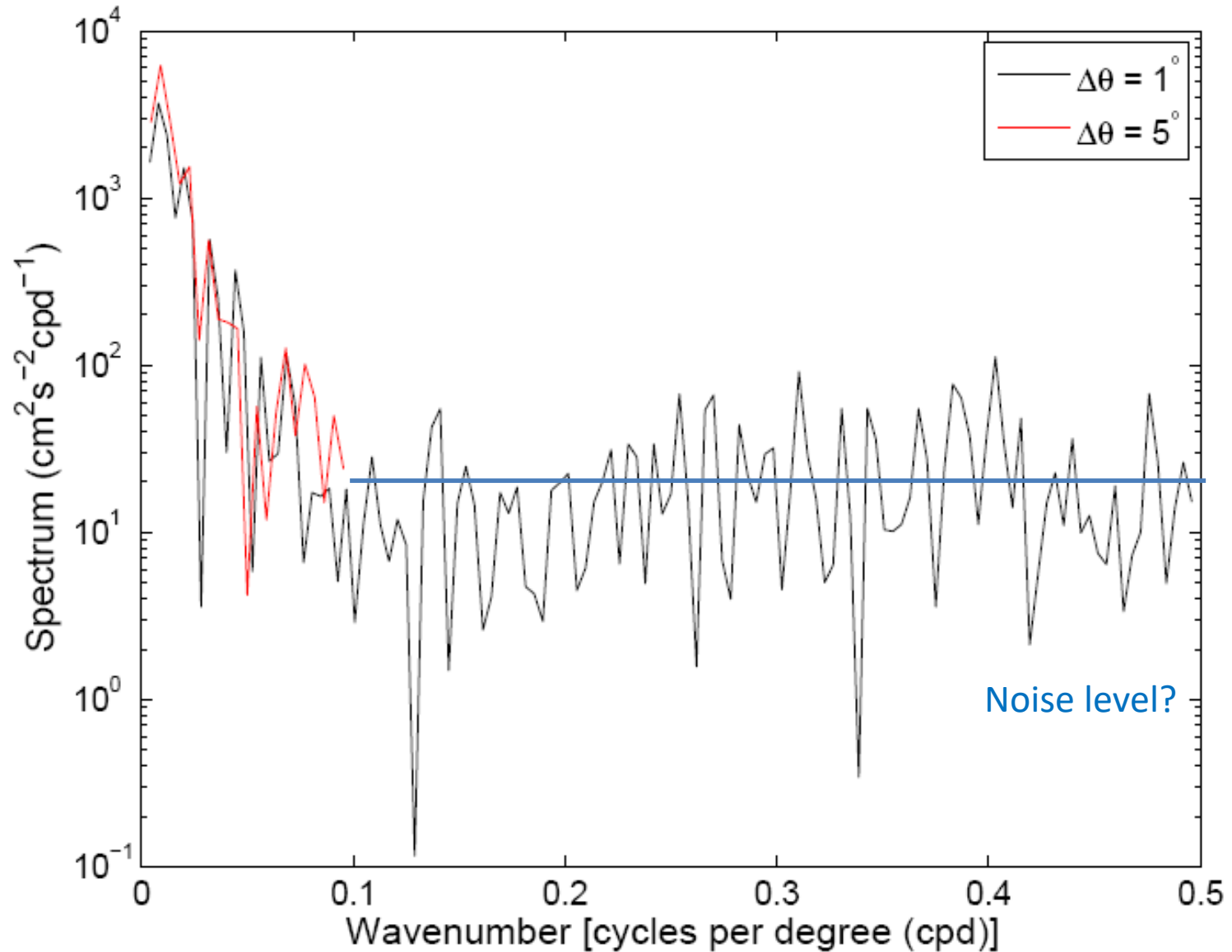
1- vs. 5-degree azimuthal resolution?



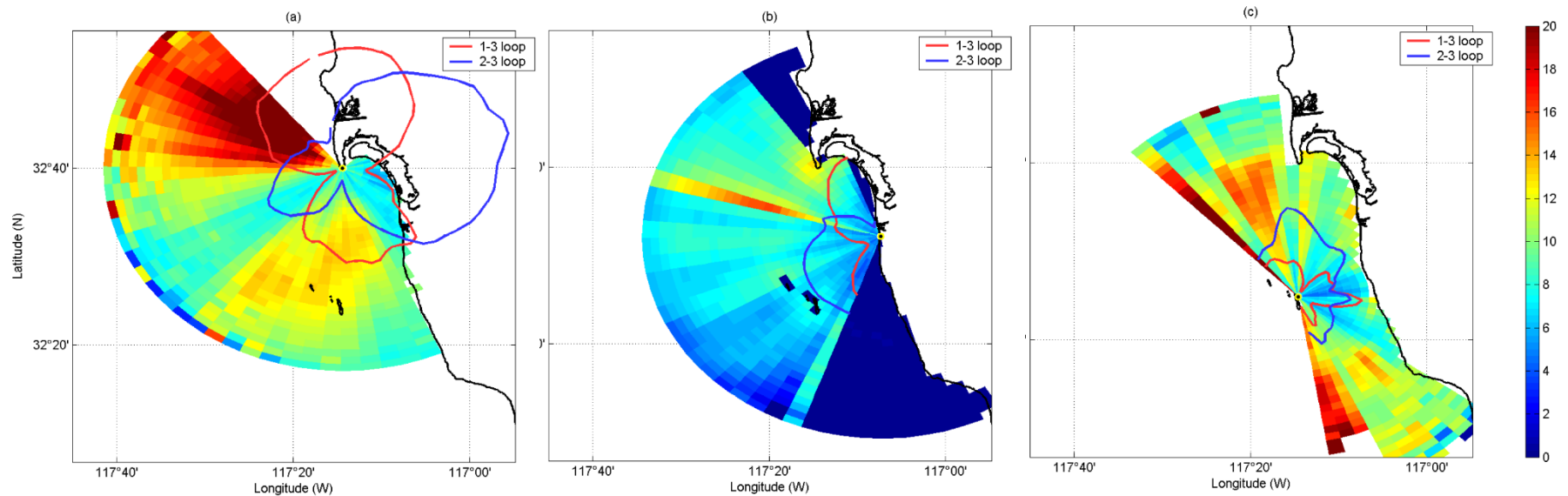
Radial velocities along a single range cell



1- vs. 5-degree azimuthal resolution?

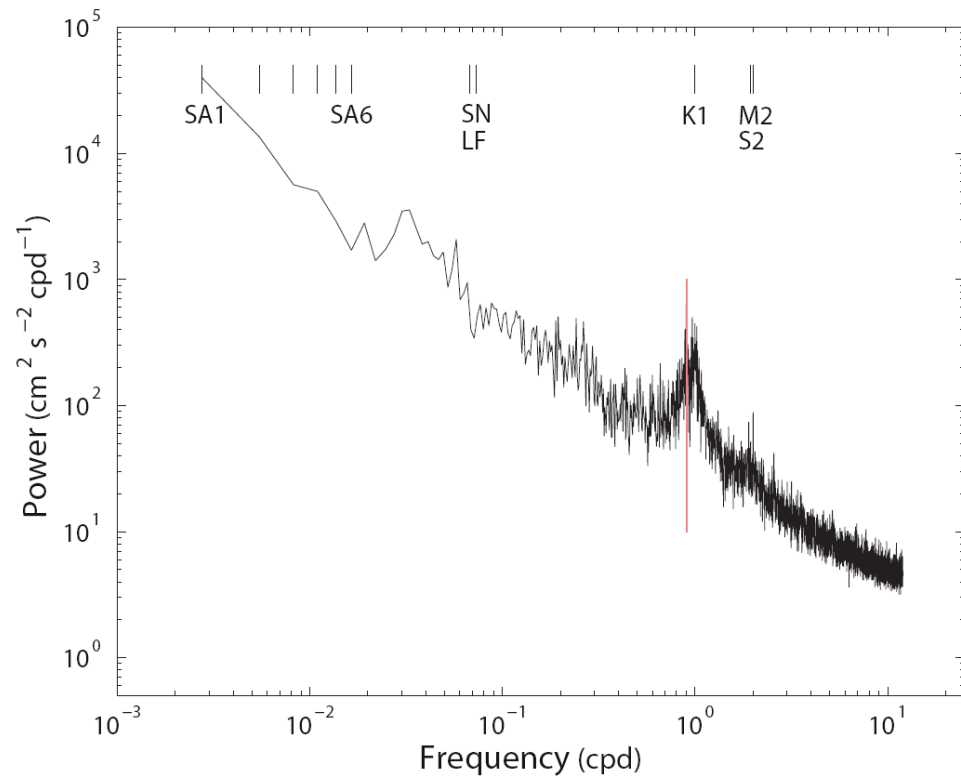
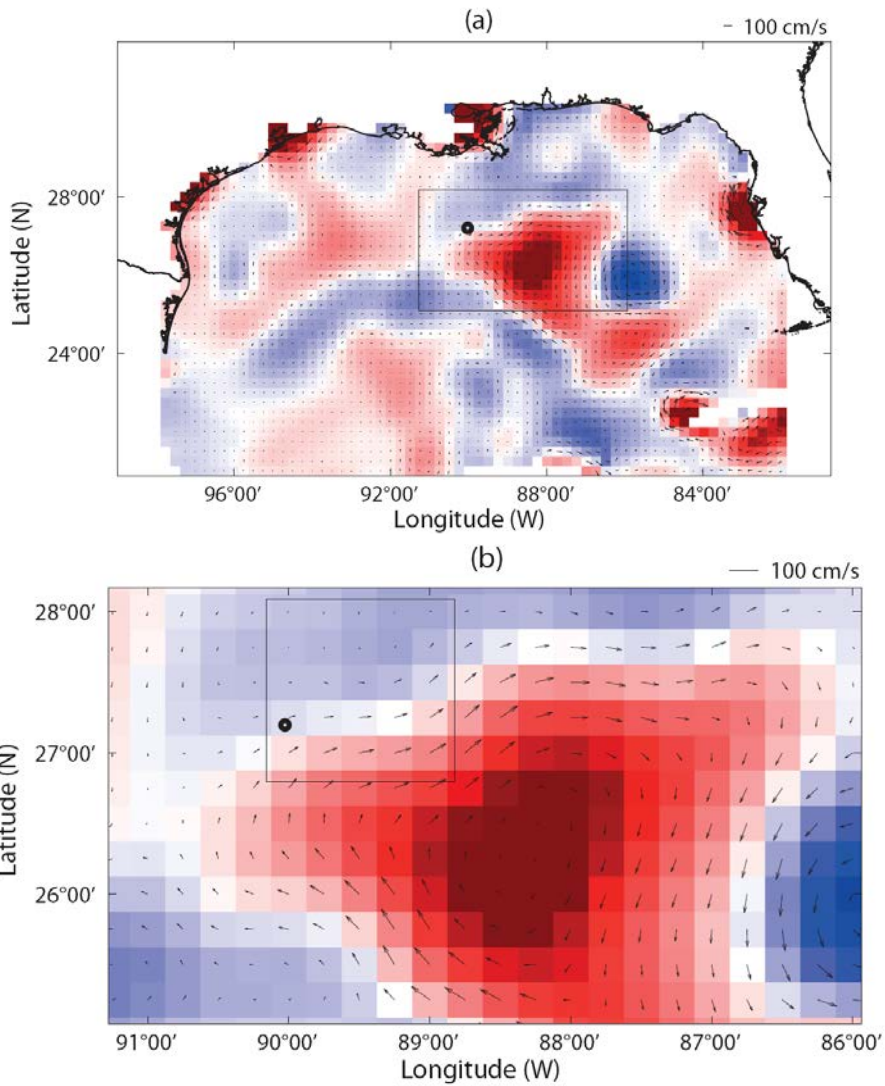


RMS of difference of radial velocity maps (ideal, measured)



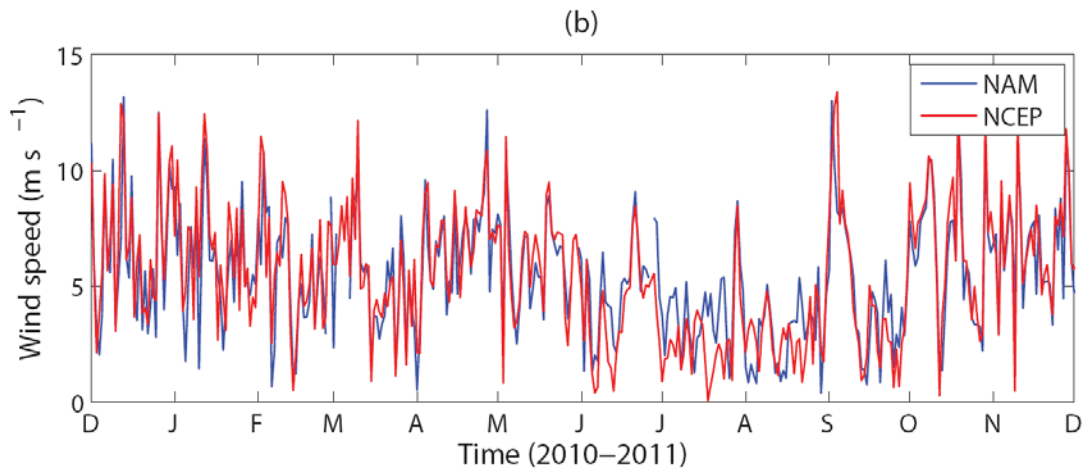
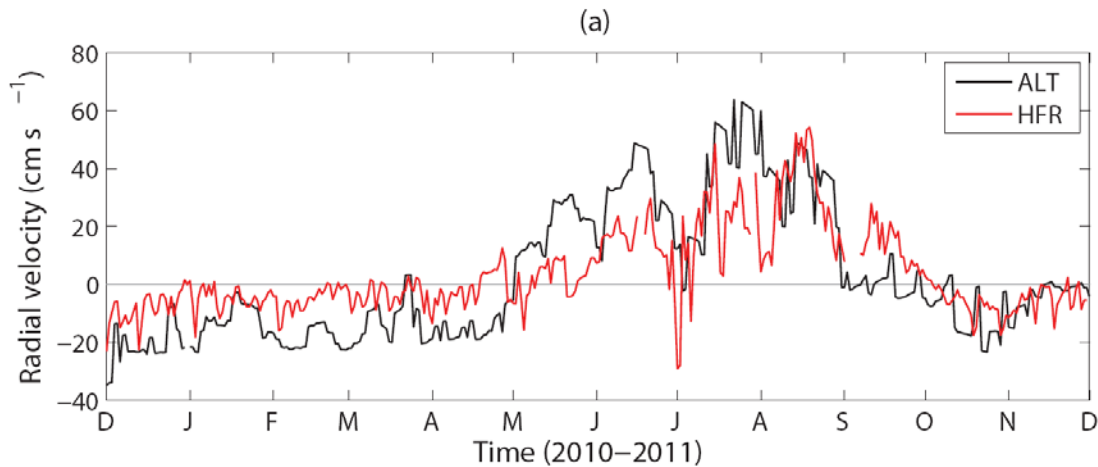
- Overlaid with radar beam pattern and rms of difference of radial velocities
- Anomalous radial velocities in an azimuthal direction with a sharp peak of the beam pattern

Geophysical signals: Energy spectra



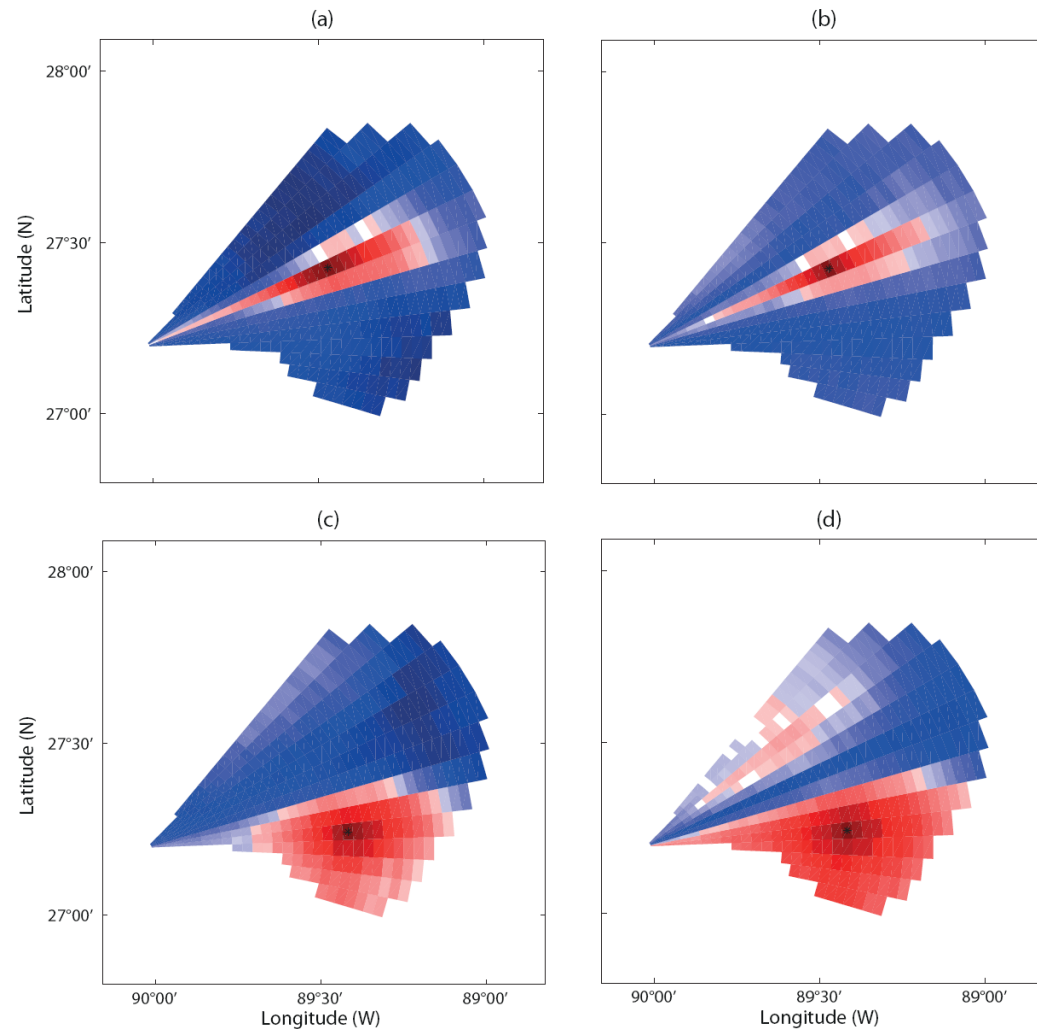
Courtesy: E. Terrill and T. Cook (SIO)

Geophysical signals: ageo-/geo-strophic currents



- CCAR/AVISO interpolated products are projected into the radial direction
- Coherent and incoherent with events; geostrophic components or potential errors

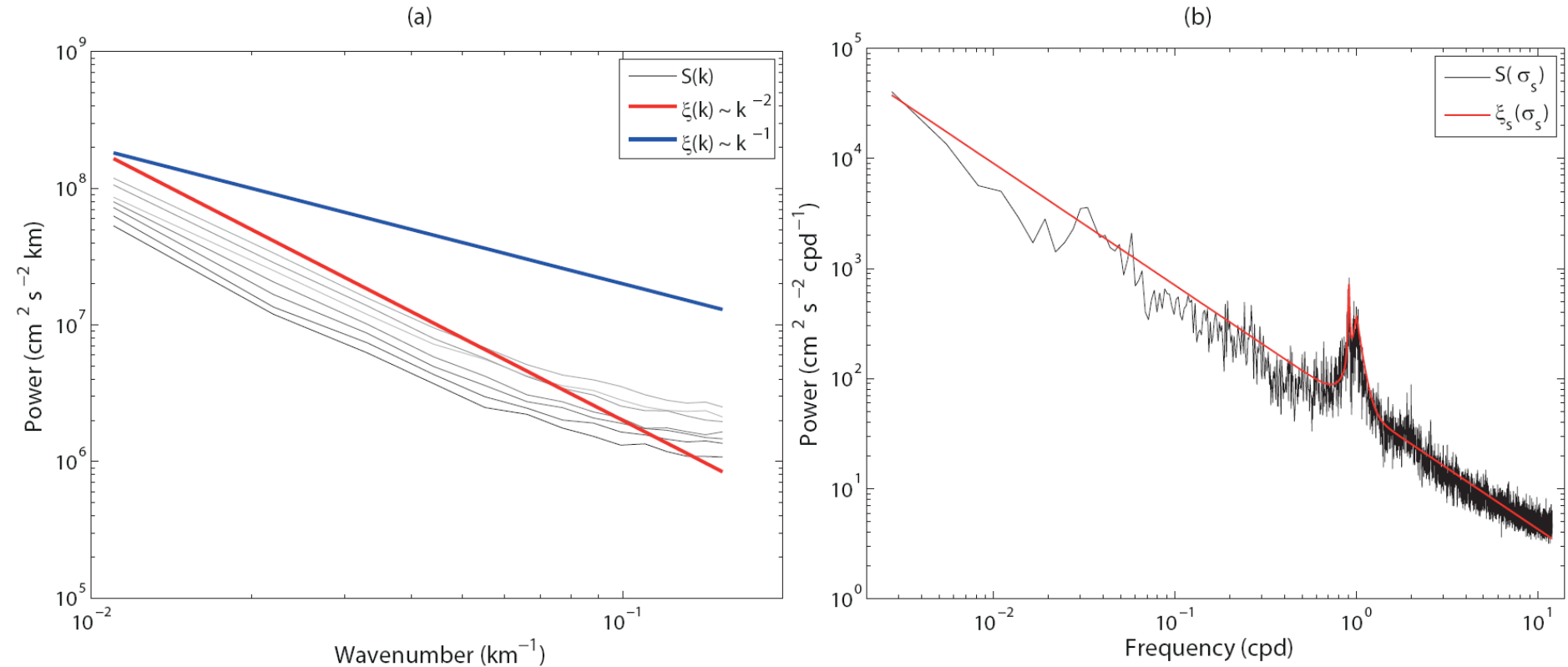
Spatial coherence: Correlation in a specific freq. band



- Spatial coherence of radial velocities in the near-inertial frequency ($|\sigma - f_c| < 0.1 f_c$) and low frequency band ($\sigma < 0.2$ cpd).
- Expected $O(100)$ km length scales for the offshore case.

$$\hat{c}(\Delta \mathbf{x}, \hat{f}_c) = \frac{\langle \hat{\mathbf{u}}(\mathbf{x}, \hat{f}_c) \hat{\mathbf{u}}^\dagger(\mathbf{x} + \Delta \mathbf{x}, \hat{f}_c) \rangle}{\sqrt{\langle |\hat{\mathbf{u}}(\mathbf{x}, \hat{f}_c)|^2 \rangle} \sqrt{\langle |\hat{\mathbf{u}}(\mathbf{x} + \Delta \mathbf{x}, \hat{f}_c)|^2 \rangle}},$$

Energy spectra of radial velocities in range and freq. domains



- Wavenumber spectra in the range direction
- Approximated energy spectra in the frequency domain

$$\xi_s(\sigma_s) = A\sigma_s^{-\alpha} + \sum_{n=1}^N B_n \exp\left(-\frac{|\sigma_s - \nu_n|}{(\lambda_t)_n}\right),$$

Summary

- **Hindcast mode QAQC** of HF radar radial velocities using statistics and geophysical consistency using long-term observations.
- Spatial coherence and energy spectra can be a first check
- Beam pattern issues may require the long-term data and reprocessing the data.
- Correlation and covariance of pairs of radial velocities can provide the noise of radar observations, which can be used in the optimal interpolation for vector current mapping.
- For **real-time mode QAQC**, the residual of the optimal interpolation can be a criteria to discern the outliers and spurious data.